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For graduate students and researchers, this self-contained account includes useful visual models to help the reader grasp abstract concepts and a list of further reading, making this the perfect reference companion on the topic.

This title, first published in 2017, has been reissued as an Open Access publication on Cambridge Core.

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