Artificial Intelligence for Engineering Design, Analysis and Manufacturing

cambridge.org/aie

A computer-aided approach improving the Axiomatic Design theory with the distributed design resource environment

Bin Chen, Jie Hu, Jin Qi and Weixing Chen

State Key Laboratory of Mechanical System and Vibration, Shanghai Jiao Tong University, Shanghai, China

Research Article

Cite this article: Chen B, Hu J, Qi J, Chen W (2020). A computer-aided approach improving the Axiomatic Design theory with the distributed design resource environment. *Artificial Intelligence for Engineering Design, Analysis and Manufacturing* **34**, 80–103. https://doi.org/10.1017/S0890060419000283

Received: 17 April 2019
Revised: 6 September 2019
Accepted: 8 September 2019
First published online: 9 October 2019

Key words:
Axiomatic Design; design resource; distributed environment; functional domain; physical domain

Authors for correspondence:
Bin Chen, E-mail: chenbinsun@outlook.com, cb5183298@sjtu.edu.cn;
Jie Hu, E-mail: hujie@sjtu.edu.cn

Abstract

In the traditional Axiomatic Design (AD) theory, the mapping from the functional domain to the physical domain is based on the designers' own knowledge and experience, and there is no systematical approach including the design resources provided outside the designers themselves' access. Thus, the raw materials for the design process are largely limited, which means they can hardly support the designers' increasingly creative and innovative conceptions. To help AD theory better support the design process, this paper proposes a computer-aided approach for the mapping from the functional domain to the physical domain within a distributed design resource environment, which consists of numerous design resources offered on the Internet by the providers widely distributed in different locations, institutes, and disciplines. To prove the feasibility of this proposed approach, a software prototype is established, and a natural leisure hotel is designed as an implementation case.

Introduction

In the Axiomatic Design (AD) theory, the design process is represented as three mappings, that is, the mapping from the customer domain to the functional domain, the mapping from the functional domain to the physical domain, and the mapping from the physical domain to the process domain. Among these three mappings, the second one is an important turning point which connects the upstream to the downstream of the design process. In this mapping, the designers should figure out proper design parameters for the functional requirements, and if they fail, they should go back to decompose the functional requirements into sub-functional requirements, and then, try to work them out. During this operation, designers should test the results whenever necessary with the independent axiom and the design matrix to find out the coupled relationships between the functional requirements and the design parameters, so that the results can be modified in time to avoid coupled relationships. If there are more than one alternatives obtained, designers should pick out the optimal one with the least information based on the information axiom. This to-and-fro process is called zigg-zagging in AD theory. It takes the main portion of the workload in a design mission. However, in the traditional AD theory, zigg-zagging between the functional domain and physical domain mainly relies on the designers' own knowledge and experience, and there is no systematical approach to help designers complete this work.

On the other hand, in the traditional AD theory, the designers can only use the design resources within their access. Maybe they can ask for help, but their sociality is also limited. If the attention can be turned to the Internet, the rich design resources offered by the outside providers would be found glaring. These design resources distributed in different locations, institutes, and disciplines. They can be connected and obtained with the help of advanced computer and Internet technologies. Thus, all these rich design resources actually construct a distributed design resource environment on the Internet. If this distributed design resource environment can be introduced into AD theory, the designers can deploy not only their design resources but also the design resources outside on the Internet.

To achieve the objective, a computer-aided approach is proposed in this study to improve the AD theory. So, the mapping from the functional domain to the physical domain can be completed within the distributed design resource environment. To prove the feasibility of this approach, a software prototype called Axiomatic Design System for Distributed Design Resource Environment (ADS-DDRE) is established, and a natural leisure hotel is designed as an implementation case. The whole study consists of three parts, that is, the classification of the design parameters, the introduction of the distributed design resource environment, and the implementation. In the rest of this paper, these three parts of work are shown, and finally, some discussions about this approach are made, and the whole work and the future study plan are also concluded.

Literature review

AD theory was first proposed by Suh (2001), and during decades of development, it is now widespread in the design community. This theory can be applied in many circumstances

© Cambridge University Press 2019

CAMBRIDGE UNIVERSITY PRESS

and disciplines. Shortly after AD theory's establishment, it was introduced into the design practice of manufacturing facilities (Suh *et al.*, 1998) and software systems (Suh and Do, 2000). Since then, a large number of researchers have been attracted to solve their design problems from multifarious domains with the help of AD theory. Cheng *et al.* (2017) developed a novel heterogeneous AD method for the anti-vibration optimization of the key components in a turbo-generator. Rauch *et al.* (2018) established a software prototype for the smart shop-floor management based on the AD theory. Product and software design is only a part of AD theory's application, AD theory is also very useful for the design problems in industrial engineering. Chen *et al.* (2018) proposed an AD method of logistics provider selection for the omnichannel environment. Rauch *et al.* (2019*b*) presented an AD method to support flexible and agile manufacturing and assembly systems for the small- and medium-sized enterprises. Additionally, AD theory's application is not limited in the engineering practice, it can also be used in social problem solving. Palleti *et al.* (2018) used the principles of AD theory to detect the vulnerabilities and corresponding potential attacks for critical infrastructures. Drakaki *et al.* (2018) addressed the refugee settlement site planning decision-making process by constructing an intelligent multi-agent system with the help of AD theory. Recently, AD theory is also actively researched and applied within the "hot" topics like sustainability and Industry 4.0. Cochran *et al.* (2016) offered an extension of AD theory to ensure that leaders, managers, and engineers can sustain manufacturing systems throughout the product lifecycle. Gualtieri *et al.* (2018) designed a collaborative human-robot workstation using AD theory for the new context of Industry 4.0. Rauch *et al.* (2019*a*) established a method to construct design guidelines for implementing Industry 4.0 learning factories using the mapping process of AD theory. Because of the limitation of the space, here just list some of the excellent works based on AD theory. More related works can be found in the review written by Rauch *et al.* (2016).

These luxuriant works in multifarious domains reemphasize that AD theory is a successful conclusion of the general rules in the design activities, and they also illustrate that the possibility of obtaining well-performed design solutions can be largely promoted if the axioms are observed. However, AD theory still needs improvement from the comprehensive consideration of engineering factors and contexts. Suh (1995) took quality into consideration to make AD theory more complete. He *et al.* (2018) introduced the consideration of sustainable and clean production into the construction of functional requirements. Chen *et al.* (2016) reconfigured AD theory within a context of knowledge service, so that demanders and suppliers could be better matched. These considerations promote the suitability of AD theory for a wider practical application; however, they also demand AD theory to be assisted by more powerful methodologies and technologies. Deo and Suh (2004) introduced mathematical transforms into the AD theory to promote the ability of description and analysis. Thielman and Ge (2006) proposed a systematic methodology to support AD theory in the evaluation and optimization of large-scale engineering systems. Li *et al.* (2019) used extenics to describe coupled solutions in the results of AD theory. These works promote AD theory's ability in description, analysis, and evaluation of design resources and solutions. However, the most important and innovative process of AD theory, the mapping from the functional domain to the physical domain, is still not accelerated efficiently. It is more and more difficult for this mapping to catch up with the increasingly comprehensive engineering considerations and the increasingly complicated description, analysis, and evaluation of design resources and solutions. To resolve this problem, researchers were attracted into the zigg-zagging between the functional domain and the physical domain, which consists of the functional requirement decomposition and the transformation from the functional requirements to the design parameters. Cochran *et al.* (2001) integrated Manufacturing System Design Decomposition (MSDD) and AD theory, so that the functional requirement decomposition can be completed by MSDD. In this way, the cost and production system design decisions become more effective (Cochran *et al.*, 2017). Yuan *et al.* (2016) completed the functional requirement decomposition with a proposed hybrid approach implemented with Systems Modeling Language (SysML). Nagel *et al.* (2009) established a functional modeling tool called FunctionCAD for the interactive functional requirement decomposition. Chakrabarti and Bligh (2001) supported the functional requirement decomposition by using the recursive problem redefinition. These works largely contribute to the functional requirement decomposition, but, as for the transformation from the functional requirements to the design parameters, it still needs more focuses.

The transformation from the functional requirements to the design parameters is tightly related to the conceptual design synthesis in other design methodologies; therefore, its acceleration can be inspired by the efforts of design synthesis automation. Vermaas and Dorst (2007) used a philosophic method to improve the model proposed by Gero for the design synthesis. Camelo and Mulet (2010) developed a multirelational and interactive model to support the design synthesis process. Welch and Dixon (1994) developed a model for conceptual design synthesis based on an explicit behavioral reasoning step. These efforts largely promote the elaboration and practicability of the conceptual design model, which means a solid foundation for the design synthesis automation. On the other hand, a well-formed representation for the elements and factors of the design process, like functional requirements, design resources, and design solutions, is also important for the design synthesis automation. Joskowicz and Neville (1996) presented a language to describe the behavior of fixed-axes mechanisms for the design synthesis of mechanisms. Stone and Wood (2000) ; and Stone *et al.* (2000) ; proposed a new design modeling language using function-flow to characterize the product function. Chen and Xie (2017*a*, 2017*b*) developed the function-flow into an input–output model to represent the function and support the automation of design synthesis. Hirtz *et al.* (2002) proposed a functional chain representation using the terminology of the functional basis for engineering design synthesis. These efforts focus on the representation of the functional requirements and design resources, if they can be considered together comprehensively, the relationships of the design resources can also be well described. As for the design solutions, some researchers introduced the graph model for help. Münzer *et al.* (2013) proposed an object-oriented and graph-based representation for computational design synthesis. Helms and Shea (2012) described the computational design synthesis process with an object-oriented graph grammar. Muenzer and Shea (2015) proposed a simulation model based on a generated concept model graph. All these efforts, like the input–output and chain-structured models for the functional requirements, the graph-based model for the design solutions, can be introduced into the traditional AD theory to make a foundation for the construction of a computer-aided approach, which can automate the transformation from the functional requirements to the design

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

parameters. Furthermore, the rich design resources offered by the outside providers should also be seriously considered, while they are usually not be paid enough attention to in the former researches about AD theory.

Classification of the design parameters

To achieve the automation of the mapping from the functional domain to the physical domain, the core mission of this study is to construct a computer-aided approach including a methodology and its corresponding algorithm, which can be executed by computers. Therefore, the main objectives, including design resources and design parameters, should be modeled as elements and their divisible attachments and constructible combinations, so that the mapping can be transformed into an executable process for a computer. Based on this idea, different design parameters may have different constructive granularities. Therefore, a classification is established in this study to distinguish the design parameters' constructive granularities, so that the design parameters can be treated respectively for the establishment of a systematical and completely-covering methodology and its corresponding algorithm.

Before the introduction of this classification, a simple design case completed by the traditional AD theory is illustrated step by step firstly to show the background.

Design case completed by the traditional AD theory

Here take a case simplified from the elevator design proposed by Xiao and Cheng (2006) as an example. As shown in Figure 1, the zigg-zagging in the middle of the figure completes the mapping from the functional domain to the physical domain. The details of the functional requirements and their corresponding design parameters are shown in Table 1. Their relationships are shown as the following design equations with design matrices.

$$\begin{bmatrix} \mathrm{FR1} \\ \mathrm{FR2} \\ \mathrm{FR3} \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ X & X & 0 \\ X & X & X \end{bmatrix} \begin{bmatrix} \mathrm{DP1} \\ \mathrm{DP2} \\ \mathrm{DP3} \end{bmatrix}, \tag{1}$$

$$\begin{bmatrix} \mathrm{FR11} \\ \mathrm{FR12} \\ \mathrm{FR13} \\ \mathrm{FR14} \end{bmatrix} = \begin{bmatrix} X & 0 & 0 & 0 \\ 0 & X & 0 & 0 \\ 0 & X & X & 0 \\ 0 & X & X & X \end{bmatrix} \begin{bmatrix} \mathrm{DP11} \\ \mathrm{DP12} \\ \mathrm{DP13} \\ \mathrm{DP14} \end{bmatrix}, \tag{2}$$

$$\begin{bmatrix} \mathrm{FR21} \\ \mathrm{FR22} \\ \mathrm{FR23} \\ \mathrm{FR24} \end{bmatrix} = \begin{bmatrix} X & 0 & 0 & 0 \\ X & X & 0 & 0 \\ X & 0 & X & 0 \\ 0 & X & 0 & X \end{bmatrix} \begin{bmatrix} \mathrm{DP21} \\ \mathrm{DP22} \\ \mathrm{DP23} \\ \mathrm{DP24} \end{bmatrix}, \tag{3}$$

$$\mathrm{FR121} = [X]\mathrm{DP121}, \tag{4}$$

$$\begin{bmatrix} \mathrm{FR141} \\ \mathrm{FR142} \\ \mathrm{FR143} \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ X & X & 0 \\ X & 0 & X \end{bmatrix} \begin{bmatrix} \mathrm{DP141} \\ \mathrm{DP142} \\ \mathrm{DP143} \end{bmatrix}. \tag{5}$$

Three kinds of design parameters

The above design case shows a situation that although the physical domain consists of design parameters, these design parameters are not always the same kind of things, they may have different essences with different constructive granularities. For example, in the above case, DP14 is "Coiling block". It is a design resource as one of the components of the final design solution. Meanwhile, DP143 is "Thickness of coiling block" which is not a design resource like DP14. Actually, it is one of DP14's features. Additionally, DP1 is different with both these two design parameters, it is actually a combination of several design resources, including "Sling", "Block and tackle", "Rope", and "Coiling block". Therefore, the design parameters can be classified into three kinds, that is, design resources (DRs), design resource features (DR Features), and design resource combinations (DR Combinations).

Design resource

Design resource is the key concept in this classification of the design parameters. Design resources are functional entities, which are the basic elements of the design solution and the raw materials for the design missions. As shown in Figure 2, a design resource is represented by its name, inputs, outputs, and features.

For a design resource, the transformation from its inputs to its outputs is defined as its function. Like the case shown in Figure 2, the design resource is a crank slider, and its function is to transform rotary motion into reciprocating motion. A design resource may have multiple inputs and outputs, and they can be described as vectors. Here assume a design resource, DR2, has m inputs, that is, $\Phi_{\mathrm{DR2}}^{\mathrm{I}(1)}, \Phi_{\mathrm{DR2}}^{\mathrm{I}(2)}, \ldots, \Phi_{\mathrm{DR2}}^{\mathrm{I}(m)}$, and n outputs, that is, $\Phi_{\mathrm{DR2}}^{\mathrm{O}(1)}, \Phi_{\mathrm{DR2}}^{\mathrm{O}(2)}, \ldots, \Phi_{\mathrm{DR2}}^{\mathrm{O}(n)}$. (In this study, the letter "Φ" is treated as the combination of the letters "I" and "O", which represents an input/output.) These inputs and outputs can be represented by the following input vector and output vector, respectively.

$$\overrightarrow{\Phi_{\mathrm{DR2}}^{\mathrm{I}}} = [\Phi_{\mathrm{DR2}}^{\mathrm{I}(1)}, \Phi_{\mathrm{DR2}}^{\mathrm{I}(2)}, \ldots, \Phi_{\mathrm{DR2}}^{\mathrm{I}(m)}]^T, \tag{6}$$

$$\overrightarrow{\Phi_{\mathrm{DR2}}^{\mathrm{O}}} = [\Phi_{\mathrm{DR2}}^{\mathrm{O}(1)}, \Phi_{\mathrm{DR2}}^{\mathrm{O}(2)}, \ldots, \Phi_{\mathrm{DR2}}^{\mathrm{O}(n)}]^T. \tag{7}$$

Thus, DR2's function, the transformation from DR2's inputs to DR2's outputs, can be represented as the following Jacobian matrix:

$$\mathrm{J}_{\mathrm{DR2}} = \frac{\partial \overrightarrow{\Phi_{\mathrm{DR2}}^{\mathrm{O}}}}{\partial \overrightarrow{\Phi_{\mathrm{DR2}}^{\mathrm{I}}}} = \begin{bmatrix} \frac{\partial \Phi_{\mathrm{DR2}}^{\mathrm{O}(1)}}{\partial \Phi_{\mathrm{DR2}}^{\mathrm{I}(1)}} & \frac{\partial \Phi_{\mathrm{DR2}}^{\mathrm{O}(1)}}{\partial \Phi_{\mathrm{DR2}}^{\mathrm{I}(2)}} & \cdots & \frac{\partial \Phi_{\mathrm{DR2}}^{\mathrm{O}(1)}}{\partial \Phi_{\mathrm{DR2}}^{\mathrm{I}(m)}} \\ \frac{\partial \Phi_{\mathrm{DR2}}^{\mathrm{O}(2)}}{\partial \Phi_{\mathrm{DR2}}^{\mathrm{I}(1)}} & \frac{\partial \Phi_{\mathrm{DR2}}^{\mathrm{O}(2)}}{\partial \Phi_{\mathrm{DR2}}^{\mathrm{I}(2)}} & \cdots & \frac{\partial \Phi_{\mathrm{DR2}}^{\mathrm{O}(2)}}{\partial \Phi_{\mathrm{DR2}}^{\mathrm{I}(m)}} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial \Phi_{\mathrm{DR2}}^{\mathrm{O}(n)}}{\partial \Phi_{\mathrm{DR2}}^{\mathrm{I}(1)}} & \frac{\partial \Phi_{\mathrm{DR2}}^{\mathrm{O}(n)}}{\partial \Phi_{\mathrm{DR2}}^{\mathrm{I}(2)}} & \cdots & \frac{\partial \Phi_{\mathrm{DR2}}^{\mathrm{O}(n)}}{\partial \Phi_{\mathrm{DR2}}^{\mathrm{I}(m)}} \end{bmatrix}. \tag{8}$$

If the integral starting point is set as 0, the effect of DR2's function can be described as the following mathematical equation:

$$\overrightarrow{\Phi_{\mathrm{DR2}}^{\mathrm{O}}} = \mathrm{J}_{\mathrm{DR2}} \overrightarrow{\Phi_{\mathrm{DR2}}^{\mathrm{I}}}. \tag{9}$$

Design resource feature

Sometimes, just a design resource feature can achieve a functional requirement, like DP143, "Thickness of coiling block", to FR143, "Bear the wrapping hoop force of the rope", shown in Figure 1 and Table 1. A design resource feature may be a design resource's

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

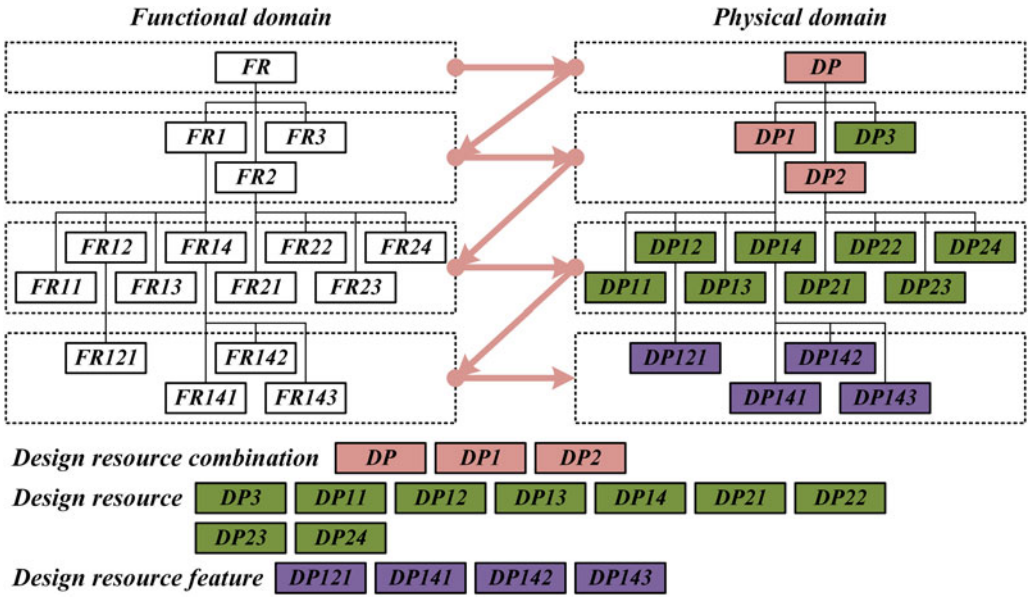


Fig. 1. Zigg-zagging between the functional domain and the physical domain.

Table 1. Functional requirements and their corresponding design parameters

FR	Elevate the stuff	DP	Elevator
FR1	Transmit the motion	DP1	Transmission
FR2	Drive the mechanism	DP2	Driving mechanism
FR3	Brake the mechanism	DP3	Brake
FR11	Link the stuff to the rope	DP11	Sling
FR12	Direct the rope, saving the labor, and increase the speed	DP12	Block and tackle
FR13	Lift the stuff	DP13	Rope
FR14	Store the rope, transform the rotation into the translation	DP14	Coiling block
FR21	Meet the power requirement of the elevator	DP21	AC motor
FR22	Meet the speed requirement of the elevator	DP22	Speed reducer
FR23	Control the speed	DP23	Speed controller
FR24	Joint the rotating axes, transmit the torque	DP24	Coupling
FR121	Save the labor and increase the speed	DP121	Multiplying power of the block and tackle
FR141	Improve the life of the rope and the structure of the speed reducer	DP141	Diameter of the coiling block
FR142	Meet the storage content of the rope	DP142	Length of the coiling block
FR143	Bear the wrapping hoop force of the rope	DP143	Thickness of coiling block

own feature, and it may also be a design resource's input or output's feature, like DP121, "Multiplying power of the block and tackle", shown in Figure 1 and Table 1. Design resource features are attachments of design resources, so that if the design resources have already been figured out for the design solution, the design resource features could directly be determined with the limited amount of workload naturally. So, in this study, the main point is establishing a way to find out the appropriate design resources and combine them into a design resource combination which can achieve the functional requirements. As for the design resource features and their corresponding functional requirements, they are not concerned much here.

Design resource combination

A design resource combination is constructed by its component design resources connecting with each other. Here, the connection among design resources is established based on the match between two inputs/outputs. Take Φ1 and Φ2 as an example, only if the following three conditions are met simultaneously, can it be determined that Φ1 matches Φ2 as the following equation:

$$\Phi 1 \overset{\text{Match}}{\rightarrow} \Phi 2. \tag{10}$$

Condition 1: Φ1 and Φ2 have the same name.

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

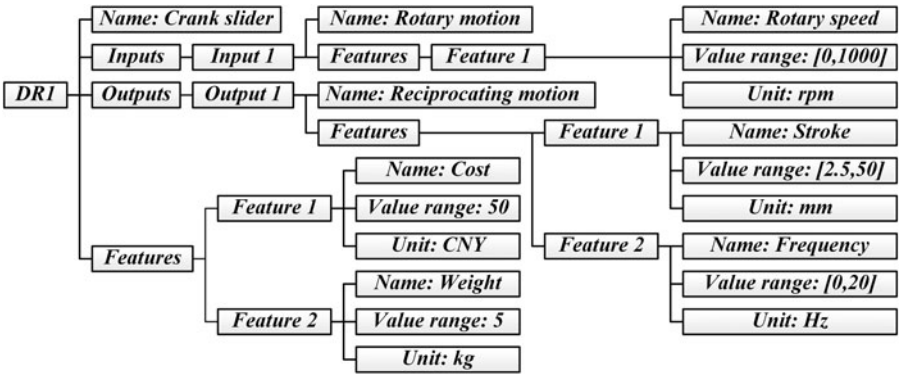


Fig. 2. Design resource and its detailed information.

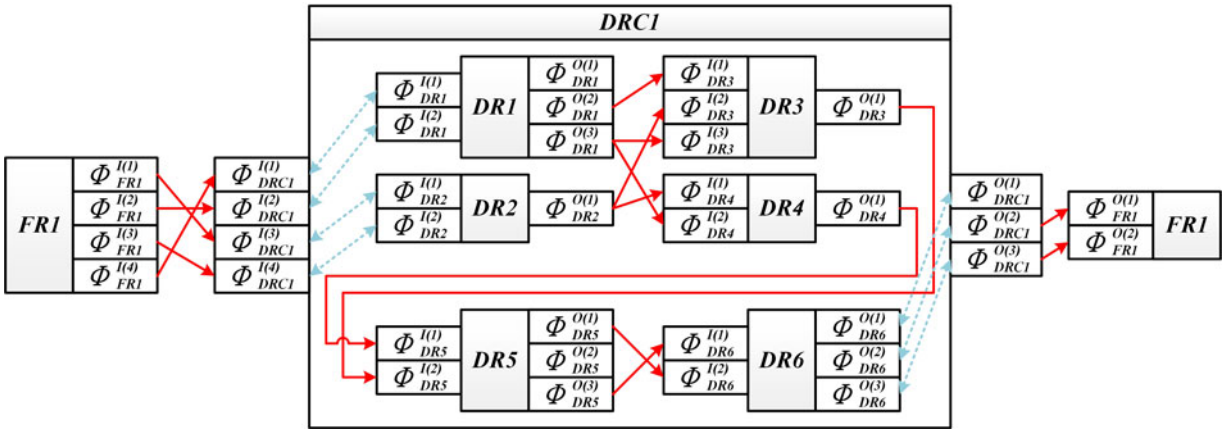


Fig. 3. Design resource combination consisting of 6 DRs.

Condition 2: Φ1's features conclude all Φ2's features.

Condition 3: For every common feature, Φ1's features have the same name and unit as Φ2's features, and the value range of Φ1's feature is contained by the value range of Φ2's feature.

Based on the above definition, design resources can be connected together into a design resource combination. Figure 3 shows an example of the design resource combination consisting of six component design resources, that is, DR1, DR2, DR3, DR4, DR5, and DR6. The matches among their inputs and outputs are shown as the following equations:

$$\Phi_{\mathrm{DR1}}^{\mathrm{O}(2)} \overset{\mathrm{Match}}{\rightarrow} \Phi_{\mathrm{DR3}}^{\mathrm{I}(1)}, \tag{11}$$

$$\Phi_{\mathrm{DR2}}^{\mathrm{O}(1)} \overset{\mathrm{Match}}{\rightarrow} \Phi_{\mathrm{DR3}}^{\mathrm{I}(2)}, \tag{12}$$

$$\Phi_{\mathrm{DR1}}^{\mathrm{O}(3)} \overset{\mathrm{Match}}{\rightarrow} \Phi_{\mathrm{DR3}}^{\mathrm{I}(3)}, \tag{13}$$

$$\Phi_{\mathrm{DR2}}^{\mathrm{O}(1)} \overset{\mathrm{Match}}{\rightarrow} \Phi_{\mathrm{DR4}}^{\mathrm{I}(1)}, \tag{14}$$

$$\Phi_{\mathrm{DR1}}^{\mathrm{O}(3)} \overset{\mathrm{Match}}{\rightarrow} \Phi_{\mathrm{DR4}}^{\mathrm{I}(2)}, \tag{15}$$

$$\Phi_{\mathrm{DR4}}^{\mathrm{O}(1)} \overset{\mathrm{Match}}{\rightarrow} \Phi_{\mathrm{DR5}}^{\mathrm{I}(1)}, \tag{16}$$

$$\Phi_{\mathrm{DR3}}^{\mathrm{O}(1)} \overset{\mathrm{Match}}{\rightarrow} \Phi_{\mathrm{DR5}}^{\mathrm{I}(2)}, \tag{17}$$

$$\Phi_{\mathrm{DR5}}^{\mathrm{O}(3)} \overset{\mathrm{Match}}{\rightarrow} \Phi_{\mathrm{DR6}}^{\mathrm{I}(1)}, \tag{18}$$

$$\Phi_{\mathrm{DR5}}^{\mathrm{O}(1)} \overset{\mathrm{Match}}{\rightarrow} \Phi_{\mathrm{DR6}}^{\mathrm{I}(2)}. \tag{19}$$

As mentioned before, a design resource's inputs and outputs can also be described as an input vector and an output vector. With this description, the connections among the design resources can also be represented as transfer matrices.

Here should first introduce the match between two input/output vectors. For two input/output vectors, $\Phi_{\mathrm{DR}x}^{\mathrm{O}}$ and $\Phi_{\mathrm{DR}y}^{\mathrm{I}}$, only if the following two conditions are met simultaneously, can it be determined that $\Phi_{\mathrm{DR}x}^{\mathrm{O}}$ matches $\Phi_{\mathrm{DR}y}^{\mathrm{I}}$ as the following equation:

$$\overrightarrow{\Phi_{\mathrm{DR}x}^{\mathrm{O}}} \overset{\mathrm{Match}}{\rightarrow} \overrightarrow{\Phi_{\mathrm{DR}y}^{\mathrm{I}}}. \tag{20}$$

Condition 1: $\overrightarrow{\Phi_{\mathrm{DR}x}^{\mathrm{O}}}$ and $\overrightarrow{\Phi_{\mathrm{DR}y}^{\mathrm{I}}}$ have the same number of vector elements.

Condition 2: The vector elements of $\overrightarrow{\Phi_{\mathrm{DR}x}^{\mathrm{O}}}$ match the vector elements of $\Phi_{\mathrm{DR}y}^{\mathrm{I}}$ one by one in order.

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

Now, go back to the connection among DR1, DR2, and DR3 shown in Equations (11)–(13). With the definition of the input/output vector match, it can also be represented by one equation in the matrix form as follows:

$$\begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} \Phi_{DR1}^{O(1)} \\ \Phi_{DR1}^{O(2)} \\ \Phi_{DR1}^{O(3)} \\ \Phi_{DR2}^{O(1)} \end{bmatrix} \overset{\text{Match}}{\rightarrow} \begin{bmatrix} \Phi_{DR3}^{I(1)} \\ \Phi_{DR3}^{I(2)} \\ \Phi_{DR3}^{I(3)} \end{bmatrix}. \tag{21}$$

Use the vector and matrix notation, this above equation can be simplified as follows:

$$C_{DR1,DR2}^{DR3} \begin{bmatrix} \overrightarrow{\Phi_{DR1}^{O}} \\ \overrightarrow{\Phi_{DR2}^{O}} \end{bmatrix} \overset{\text{Match}}{\rightarrow} \overrightarrow{\Phi_{DR3}^{I}}. \tag{22}$$

Here, $C_{DR1,DR2}^{DR3}$ represents the transfer matrix of the connection from DR1 and DR2 to DR3. Based on this description, the other design resource connections can be represented as follows:

$$C_{DR1,DR2}^{DR4} \begin{bmatrix} \overrightarrow{\Phi_{DR1}^{O}} \\ \overrightarrow{\Phi_{DR2}^{O}} \end{bmatrix} \overset{\text{Match}}{\rightarrow} \overrightarrow{\Phi_{DR4}^{I}}, \quad C_{DR1,DR2}^{DR4} = \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}, \tag{23}$$

$$C_{DR3,DR4}^{DR5} \begin{bmatrix} \overrightarrow{\Phi_{DR3}^{O}} \\ \overrightarrow{\Phi_{DR4}^{O}} \end{bmatrix} \overset{\text{Match}}{\rightarrow} \overrightarrow{\Phi_{DR5}^{I}}, \quad C_{DR3,DR4}^{DR5} = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}, \tag{24}$$

$$C_{DR5}^{DR6} \overrightarrow{\Phi_{DR5}^{I}} \overset{\text{Match}}{\rightarrow} \overrightarrow{\Phi_{DR6}^{I}}, \quad C_{DR5}^{DR6} = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix}. \tag{25}$$

As the design resources in the design resource combination connect with each other, the design resource combination itself also connect with the functional requirement. This connection can also be described by the matches among the inputs and outputs of the design resource combination and the functional requirement. Here define the inputs of the upstream design resources as the inputs of the whole design resource combination, and the outputs of the downstream design resources as the outputs of the whole design resource combination. The situation in this case is shown as the following equations:

$$\Phi_{DRC1}^{I(1)} = \Phi_{DR1}^{I(1)}, \tag{26}$$

$$\Phi_{DRC1}^{I(2)} = \Phi_{DR1}^{I(2)}, \tag{27}$$

$$\Phi_{DRC1}^{I(3)} = \Phi_{DR2}^{I(1)}, \tag{28}$$

$$\Phi_{DRC1}^{I(4)} = \Phi_{DR2}^{I(2)}, \tag{29}$$

$$\Phi_{DRC1}^{O(1)} = \Phi_{DR6}^{O(1)}, \tag{30}$$

$$\Phi_{DRC1}^{O(2)} = \Phi_{DR6}^{O(2)}, \tag{31}$$

$$\Phi_{DRC1}^{O(3)} = \Phi_{DR6}^{O(3)}. \tag{32}$$

Therefore, the connection between the functional resource combination and the functional requirement shown in Figure 3 can be described as the following input/output matches:

$$\Phi_{FR1}^{I(4)} \overset{\text{Match}}{\rightarrow} \Phi_{DRC1}^{I(1)}, \tag{33}$$

$$\Phi_{FR1}^{I(2)} \overset{\text{Match}}{\rightarrow} \Phi_{DRC1}^{I(2)}, \tag{34}$$

$$\Phi_{FR1}^{I(1)} \overset{\text{Match}}{\rightarrow} \Phi_{DRC1}^{I(3)}, \tag{35}$$

$$\Phi_{FR1}^{I(3)} \overset{\text{Match}}{\rightarrow} \Phi_{DRC1}^{I(4)}, \tag{36}$$

$$\Phi_{DRC1}^{O(2)} \overset{\text{Match}}{\rightarrow} \Phi_{FR1}^{O(1)}, \tag{37}$$

$$\Phi_{DRC1}^{O(3)} \overset{\text{Match}}{\rightarrow} \Phi_{FR1}^{O(2)}. \tag{38}$$

Use the vector and matrix representation, the above equations, Equations (26)–(38), can be concluded as the following two equations:

$$C_{FR1}^{DRC1} \overrightarrow{\Phi_{FR1}^{I}} \overset{\text{Match}}{\rightarrow} \overrightarrow{\Phi_{DRC1}^{I}} = \begin{bmatrix} \overrightarrow{\Phi_{DR1}^{I}} \\ \overrightarrow{\Phi_{DR2}^{I}} \end{bmatrix}, \quad C_{FR1}^{DRC1} = \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}, \tag{39}$$

$$C_{DRC1}^{FR1} \overrightarrow{\Phi_{DRC1}^{O}} = C_{DRC1}^{FR1} \overrightarrow{\Phi_{DR6}^{O}} \overset{\text{Match}}{\rightarrow} \overrightarrow{\Phi_{FR1}^{O}}, \quad C_{DRC1}^{FR1} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}. \tag{40}$$

Introducing the distributed design resource environment

As mentioned before, this study is mainly focused on the design resource searching and design resource combination constructing, as for the design resource features and their corresponding functional requirements, they are not concerned much here. To achieve this main goal, a computer-aided approach is proposed for the mapping from the functional domain to the physical domain. This approach takes the rich design resources outside the designers' access into consideration and also includes a

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

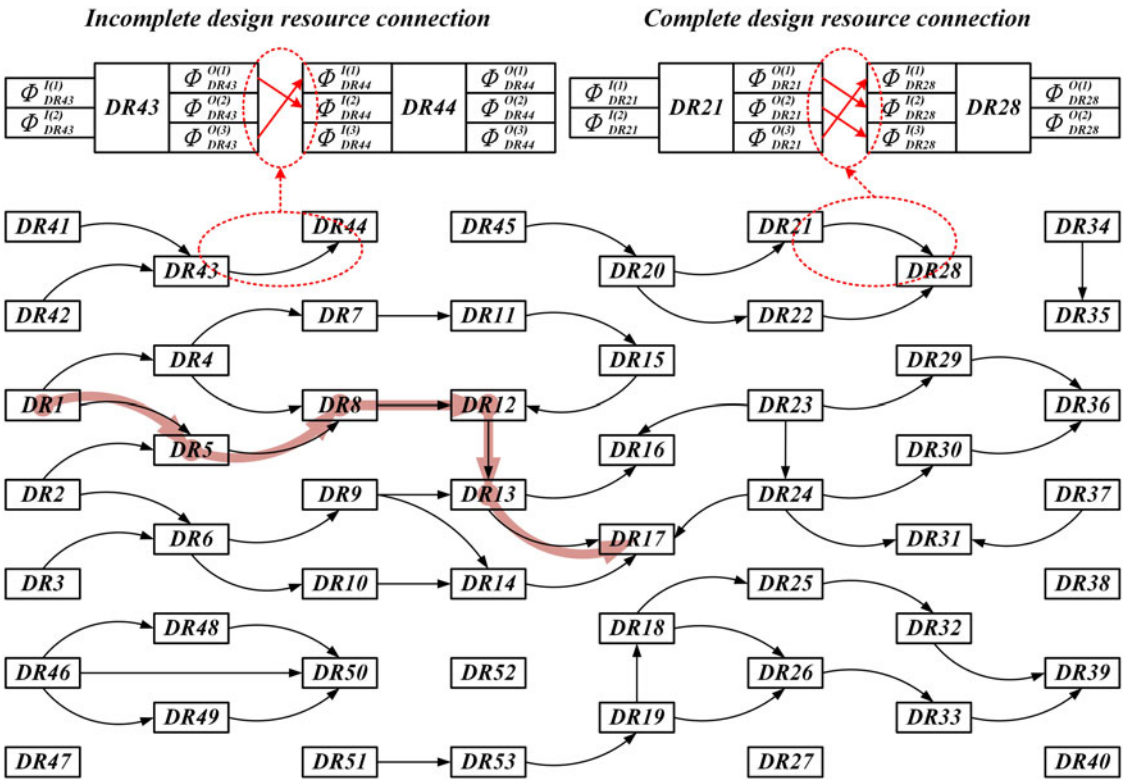


Fig. 4. Design resource graph and the incomplete design resource connection.

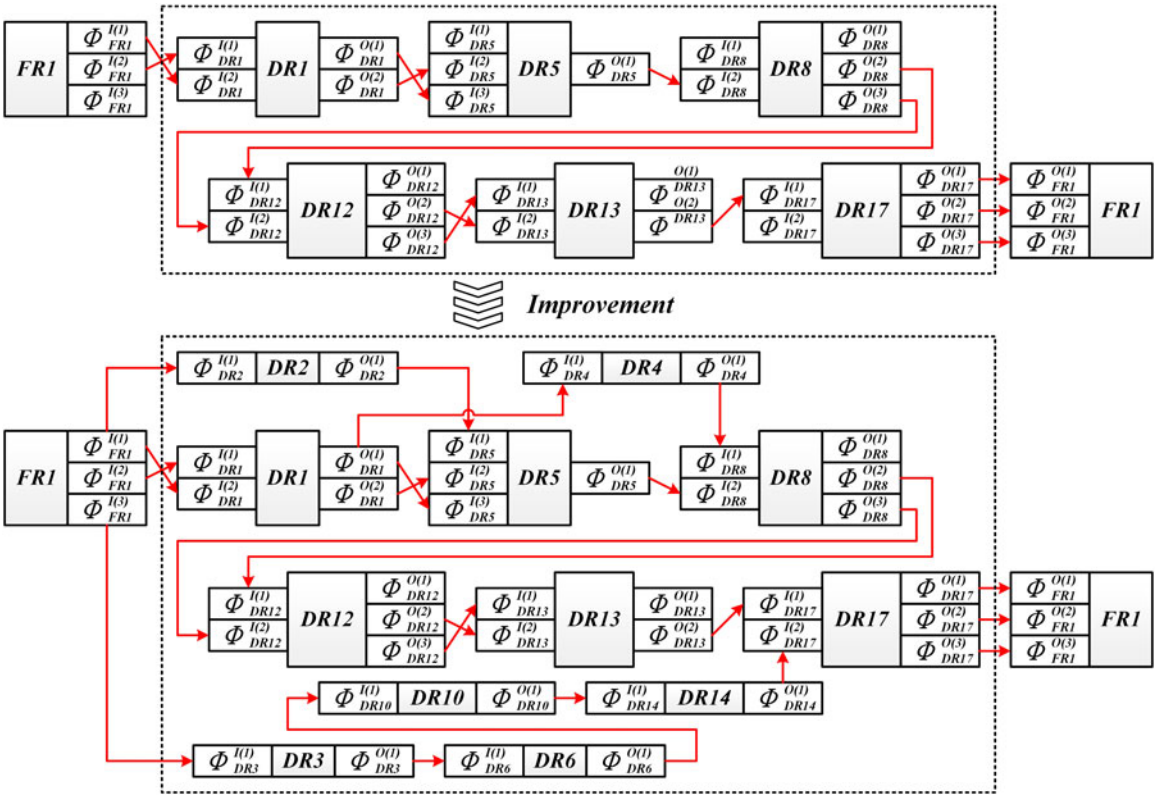


Fig. 5. Constructing the final design resource combination by adding assistant design resources into the design resource chain.

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

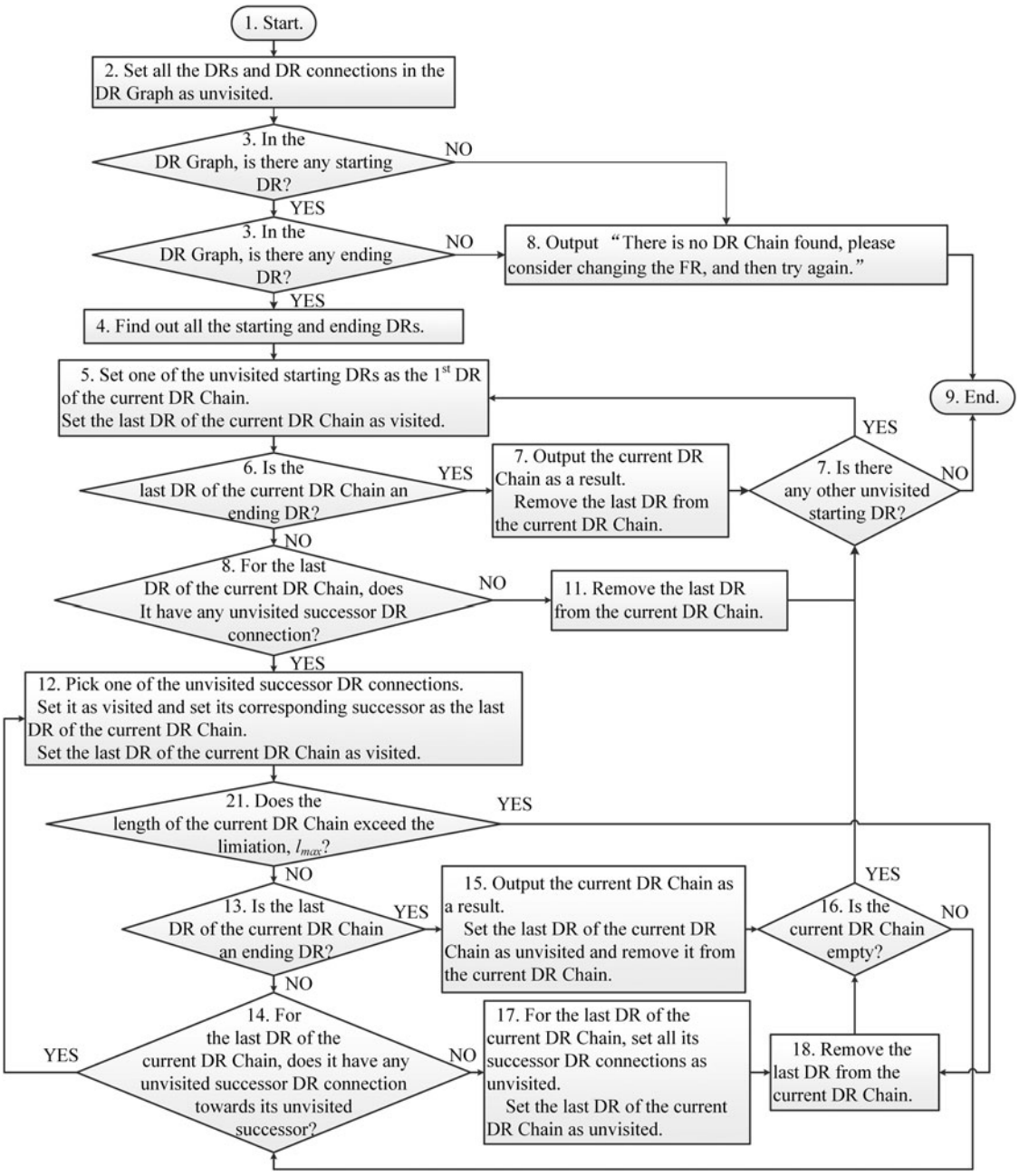


Fig. 6. Flow diagram of the design resource chain generating algorithm.

computer algorithm to help complete the mechanical and repetitive works of design resource searching and design resource combination exhausting. This approach can improve AD theory's support for the designers, and alleviate the contradiction between the designers' increasingly innovative design conception and the limitation of their access to the rich design resources and the powerful computing capacity.

This proposed approach obtains access to the outside design resources via the advanced Internet. The design resources can be published on the Internet by their providers distributed in different locations, institutes, and disciplines. These design resources on the Internet actually construct a distributed design resource environment, and the proposed approach plays the role of a bridge connecting this environment and the designers. To achieve this, the distributed design resource environment is firstly modeled as a design resource graph, so that its design resources can be searched and combined by a computer algorithm based on the functional requirement.

Design resource graph

Design resource graph is a data model of the distributed design resource environment. It records the design resources and their connections as shown in Figure 4. However, the connections in the design resource graph are not necessarily complete. In this design resource graph, the connection from DR43 to DR44 is incomplete because the third input of DR44 is not matched by any output of DR43. This flexible and slack constructive

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

Table 2. Operating steps of the design resource chain generating algorithm and the corresponding changes of the generated design resource chain

Step	Current DR chain	Description
1	Ø	In the beginning, the current DR Chain is empty.
2	DR1	Set one of the starting DRs as the 1st DR of the current DR Chain.
3	DR1>DR4	Find DR1's successors, and set one of them as the 2nd DR of the current DR Chain.
4	DR1>DR4>DR7	Find DR4's successors, and set one of them as the 3rd DR of the current DR Chain.
5	DR1>DR4>DR7>DR11	DR7 has only one successor, so set this successor as the 4th DR of the current DR Chain.
6	DR1>DR4>DR7>DR11>DR15	DR11 has only one successor, so set this successor as the 5th DR of the current DR Chain.
7	DR1>DR4>DR7>DR11>DR15>DR12	DR15 has only one successor, so set this successor as the 6th DR of the current DR Chain.
8	DR1>DR4>DR7>DR11>DR15>DR12>DR13	DR12 has only one successor, so set this successor as the 7th DR of the current DR Chain.
9	DR1>DR4>DR7>DR11>DR15>DR12	The length of the current DR Chain exceeds the limitation (6 DRs), so remove the last DR.
10	DR1>DR4>DR7>DR11>DR15	DR12 has no other successor, so remove it.
11	DR1>DR4>DR7>DR11	DR15 has no other successor, so remove it.
12	DR1>DR4>DR7	DR11 has no other successor, so remove it.
13	DR1>DR4	DR7 has no other successor, so remove it.
14	DR1>DR4>DR8	DR4 has another successor, so set this successor as the 3rd DR of the current DR Chain.
15	DR1>DR4>DR8>DR12	DR8 has only one successor, so set this successor as the 4th DR of the current DR Chain.
16	DR1>DR4>DR8>DR12>DR13	DR12 has only one successor, so set this successor as the 5th DR of the current DR Chain.
17	DR1>DR4>DR8>DR12>DR13>DR16	Find DR13's successors, and set one of them as the 6th DR of the current DR Chain.
18	DR1>DR4>DR8>DR12>DR13	DR16 has no successor, so remove it.
19	DR1>DR4>DR8>DR12>DR13>DR17	DR13 has another successor, so set this successor as the 6th DR of the current DR Chain.
20	DR1>DR4>DR8>DR12>DR13	DR17 is the ending DR, so output the current DR Chain as a result, and then, remove the last DR.
21	DR1>DR4>DR8>DR12	DR13 has no other successor, so remove it.
22	DR1>DR4>DR8	DR12 has no other successor, so remove it.
23	DR1>DR4	DR8 has no other successor, so remove it.
24	DR1	DR4 has no other successor, so remove it.
25	DR1>DR5	DR1 has another successor, so set this successor as the 2nd DR of the current DR Chain.
26	DR1>DR5>DR8	DR5 has only one successor, so set this successor as the 3rd DR of the current DR Chain.
27	DR1>DR5>DR8>DR12	DR8 has only one successor, so set this successor as the 4th DR of the current DR Chain.
28	DR1>DR5>DR8>DR12>DR13	DR12 has only one successor, so set this successor as the 5th DR of the current DR Chain.
29	DR1>DR5>DR8>DR12>DR13>DR16	Find DR13's successors, and set one of them as the 6th DR of the current DR Chain.
30	DR1>DR5>DR8>DR12>DR13	DR16 has no successor, so remove it.
31	DR1>DR5>DR8>DR12>DR13>DR17	DR13 has another successor, so set this successor as the 6th DR of the current DR Chain.
32	DR1>DR5>DR8>DR12>DR13	DR17 is the ending DR, so output the current DR Chain as a result, and then, remove the last DR.
33	DR1>DR5>DR8>DR12	DR13 has no other successor, so remove it.
34	DR1>DR5>DR8	DR12 has no other successor, so remove it.
35	DR1>DR5	DR8 has no other successor, so remove it.
36	DR1	DR5 has no other successor, so remove it.
37	Ø	DR1 has no other successor, so remove it.
38	DR3	Set another starting DR as the 1st DR of the current DR Chain and repeat the above process.
…	…	…

The design resource graph is shown in Figure 4. DR1 and DR3 are the starting design resources, and DR17 is the ending design resource. The limitation of the generated design resource chain's length is 6 DRs.

configuration of design resource graph is suitable for the two-step construction of a design resource combination. In the first step, a chain of design resources is searched out from the design resource graph with a computer algorithm which is proposed in the Design resource chain generating algorithm section. This chain is completely connected with the functional requirement via its starting

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

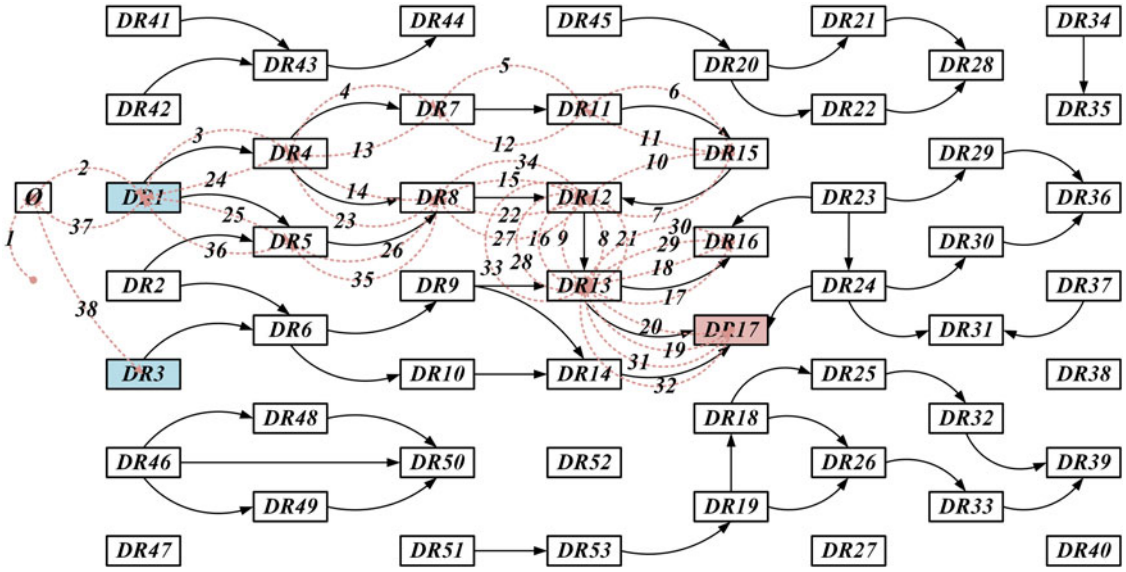


Fig. 7. Illustration of the operating steps of the design resource chain generating algorithm.

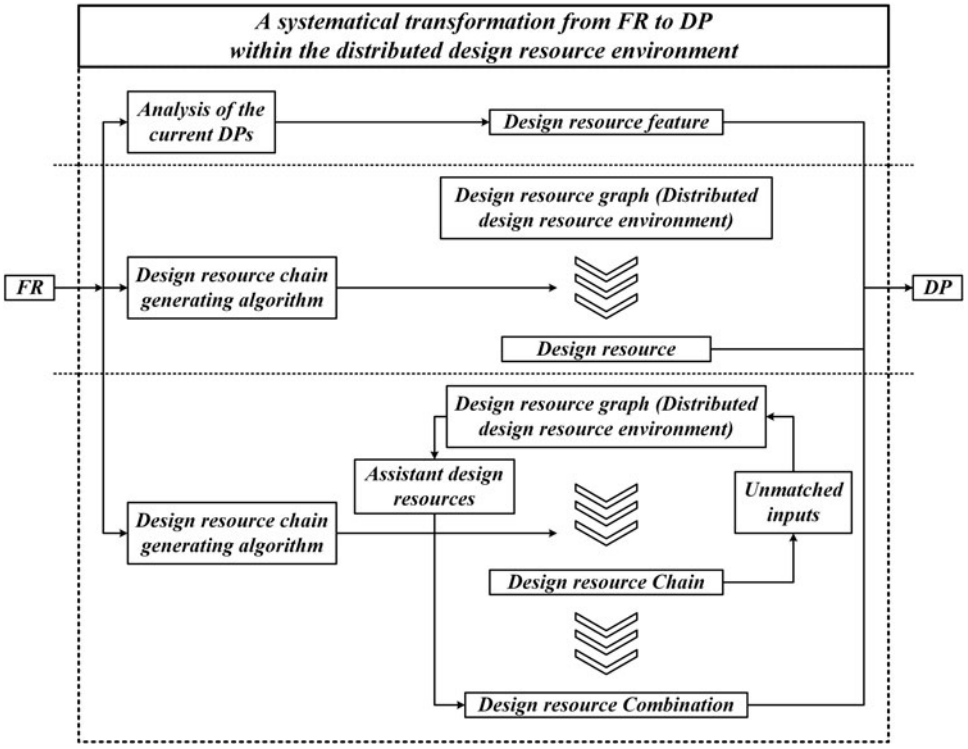


Fig. 8. Systematical transformation from the functional requirements to the design parameters.

design resource as the upstream design resource and the ending design resource as the downstream design resource. Meanwhile, the connections among its component design resources are not necessarily complete, so that there is the possibility of adding assistant design resources into this chain and improving it into a non-chain-shaped design resource combination in the second step. Therefore, the structures of constructed design resource combinations are not limited as chains, which flourishes the diversity of the construction's results.

Assume the chain signed in Figure 4, that is, DR1→DR5→DR8→DR12→DR13→DR17, is obtained in the first step, and its detailed input/output matching situation is shown in Figure 5. In this chain, there are three unmatched design resource inputs, that is, the first input of DR5, the first input of DR8, and the second input of DR17. This design resource chain cannot achieve the functional requirement unless these inputs are all matched. Therefore, six assistant design resources are found out from the design resource graph, and added into the design

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

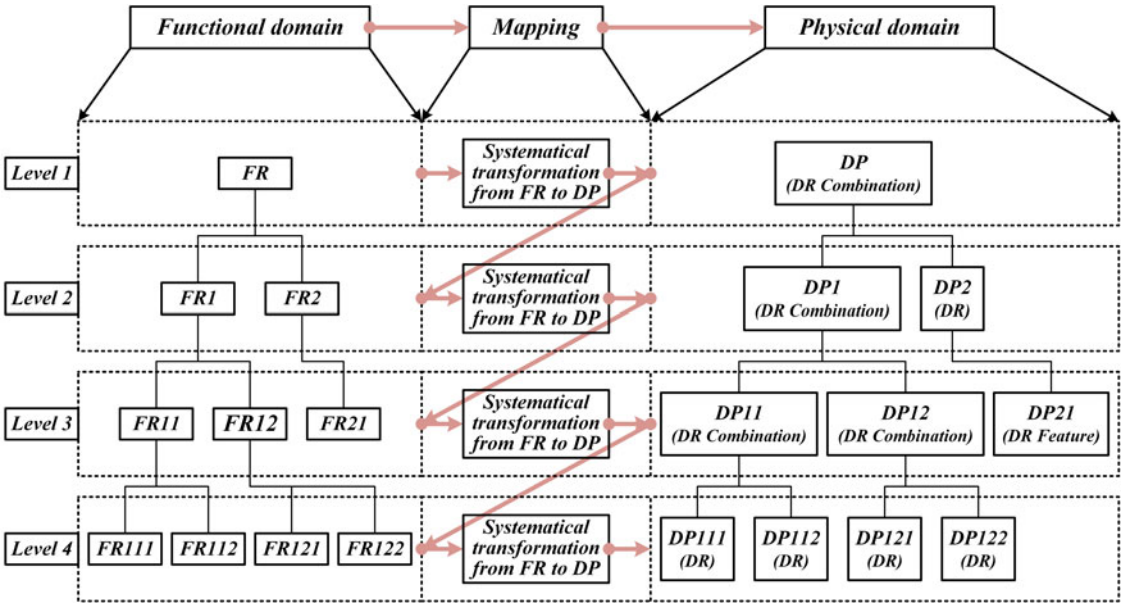


Fig. 9. Computer-aided approach for the mapping from the functional domain to the physical domain.

Table 3. Detailed information of FR0

Functional requirement	Input and output vectors		Inputs and outputs			
			Name	Features		
				Name	Value range	Unit
FR0	$\overrightarrow{X^{I}_{FR0}} = \begin{bmatrix} X^{I(1)}_{FR0} \\ X^{I(2)}_{FR0} \\ X^{I(3)}_{FR0} \\ X^{I(4)}_{FR0} \\ X^{I(5)}_{FR0} \end{bmatrix}$	$X^{I(1)}_{FR0}$	Sunlight	Illumination intensity	[60,000, 100,000]	lx
				Color temperature	[5000.0, 7000.0]	K
				Frequency	[510.0, 530.0]	Hz
				Energy density	[800.0, 1200.0]	W/m^2
		$X^{I(2)}_{FR0}$	River flow	Flow velocity	[0.8, 2.0]	m/s
				Flow rate	[0.65, 1.87]	m^3/s
		$X^{I(3)}_{FR0}$	Daily garbage	Water content	[15.0, 85.0]	%
				Particle diameter	[0.5, 800.0]	mm
		$X^{I(4)}_{FR0}$	Maize straw	Density	[800.0, 1400.0]	kg/m^3
				Ash content	[1.0, 10.0]	%
				Water content	[2.0, 15.0]	%
				Caloricity	[3700.0, 5000.0]	kcal
		$X^{I(5)}_{FR0}$	Organic food	Null		
	$\overrightarrow{X^{O}_{FR0}} = [X^{O(1)}_{FR0}]$	$X^{O(1)}_{FR0}$	Natural leisure services	Null		

resource chain, so that the three inputs are matched, and the final non-chain-shaped design resource combination is formed.

Design resource chain generating algorithm

As mentioned in the Design resource graph section, a computer algorithm is proposed in this study to generate design resource chains from the design resource graph. These chains' starting and ending design resources should completely connect with the functional requirement, which means only some of the design resources in the design resource graph can play the role of the starting and ending design resources. Therefore, the following two criteria are proposed to determine whether a design resource can serve as the starting or ending design resource of the generated design resource chain (DR Chain).

DR Chain Criterion 1

For a design resource, if all its inputs can be matched by the inputs of the functional requirement, it can be determined

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

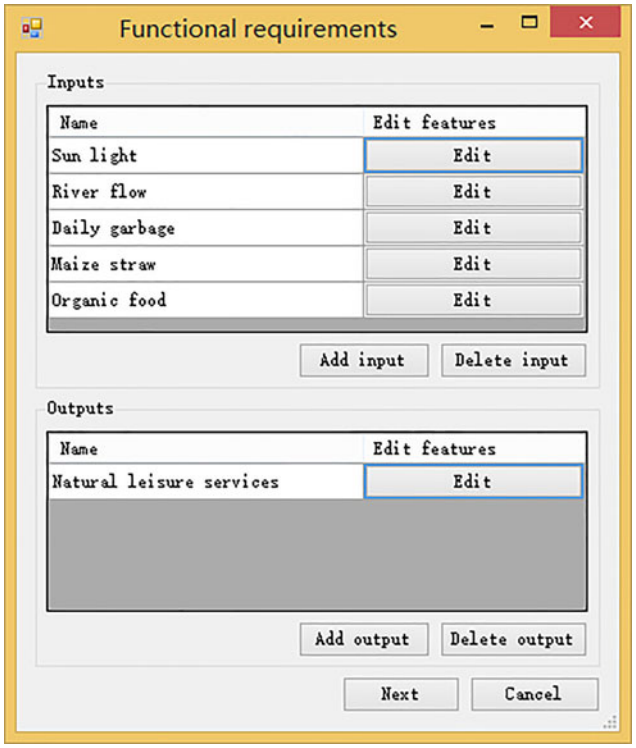


Fig. 10. Inputting FR0 into ADS-DDRE.

as a starting design resource of the generated design resource chain.

DR Chain Criterion 2

For a design resource, if all the functional requirement's outputs can be matched by its outputs, it can be determined as an ending design resource of the generated design resource chain.

During the design resource chain generating algorithm, all the starting and ending design resources should be found out first, and then, the next work is about figuring out design-resource-formed paths bridging any pair of starting and ending design resources. This process can be described as the following steps:

Step 1. In the beginning, the generated design resource chain is empty. Add one of the starting design resources into the generated design resource chain as the 1st design resource.

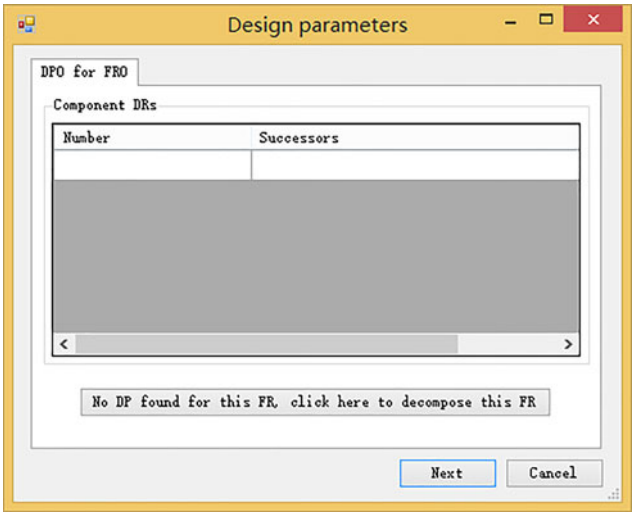


Fig. 12. No proper design parameter is found for FR0.

Step 2. Find out all the successors of the 1st design resource, and add one of them into the generated design resource chain as the 2nd design resource.

Step 3. Keep on finding the successors of the generated design resource chain's last design resource, so that the chain keeps growing longer.

Step 4. Interrupt the design resource chain's growth when one of the following three situations occurs.

(1) The length of the generated design resource chain exceeds the limitation which is set to avoid overlong design resource chains.
(2) The generated design resource chain's last design resource has no successor.
(3) The generated design resource chain's last design resource is an ending design resource.

Among these three situations, only the last one indicates that a proper design resource chain is found successfully. So, the generated design resource chain should be outputted as a result.

Step 5. After the interrupt mentioned in Step 4, the generated design resource chain's last design resource should be removed. If the generated design resource chain's new last design resource has

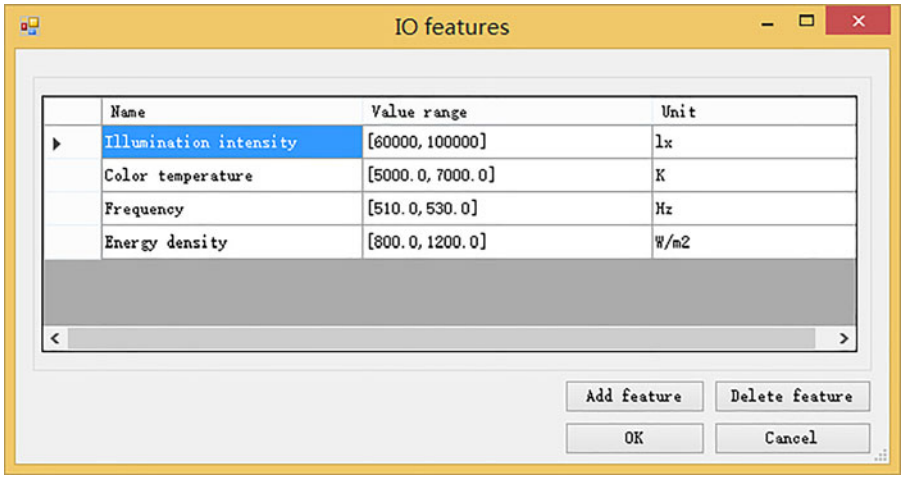


Fig. 11. Editing the features of FR0's inputs and outputs.

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

Table 4. Detailed information of FR01 and FR02

Functional requirement	Input and output vectors	Inputs and outputs				
			Name	Features		
				Name	Value range	Unit
FR01	$\overrightarrow{X^{I}_{FR01}} = \begin{bmatrix} X^{I(1)}_{FR01} \\ X^{I(2)}_{FR01} \\ X^{I(3)}_{FR01} \\ X^{I(4)}_{FR01} \\ X^{I(5)}_{FR01} \end{bmatrix}$	$X^{I(1)}_{FR01}$	Sunlight	Illumination intensity	[60,000, 100,000]	lx
				Color temperature	[5000.0, 7000.0]	K
				Frequency	[510.0, 530.0]	Hz
				Energy density	[800.0, 1200.0]	W/m^2
		$X^{I(2)}_{FR01}$	River flow	Flow velocity	[0.8, 2.0]	m/s
				Flow rate	[0.65, 1.87]	m^3/s
		$X^{I(3)}_{FR01}$	Daily garbage	Water content	[15.0, 85.0]	%
				Particle diameter	[0.5, 800.0]	mm
		$X^{I(4)}_{FR01}$	Maize straw	Density	[800.0, 1400.0]	kg/m^3
				Ash content	[1.0, 10.0]	%
				Water content	[2.0, 15.0]	%
				Caloricity	[3700.0, 5000.0]	kcal
		$X^{I(5)}_{FR01}$	Organic food	Null		
	$\overrightarrow{X^{O}_{FR0}} = [X^{O(1)}_{FR01}]$	$X^{O(1)}_{FR01}$	Natural residence	Null		
FR02	$\overrightarrow{X^{I}_{FR02}} = \begin{bmatrix} X^{I(1)}_{FR02} \\ X^{I(2)}_{FR02} \\ X^{I(3)}_{FR02} \\ X^{I(4)}_{FR02} \\ X^{I(5)}_{FR02} \end{bmatrix}$	$X^{I(1)}_{FR02}$	Sunlight	Illumination intensity	[60,000, 100,000]	lx
				Color temperature	[5000.0, 7000.0]	K
				Frequency	[510.0, 530.0]	Hz
				Energy density	[800.0, 1200.0]	W/m^2
		$X^{I(2)}_{FR02}$	River flow	Flow velocity	[0.8, 2.0]	m/s
				Flow rate	[0.65, 1.87]	m^3/s
		$X^{I(3)}_{FR02}$	Daily garbage	Water content	[15.0, 85.0]	%
				Particle diameter	[0.5, 800.0]	mm
		$X^{I(4)}_{FR02}$	Maize straw	Density	[800.0, 1400.0]	kg/m^3
				Ash content	[1.0, 10.0]	%
				Water content	[2.0, 15.0]	%
				Caloricity	[3700.0, 5000.0]	kcal
		$X^{I(5)}_{FR02}$	Organic food	Null		
	$\overrightarrow{X^{O}_{FR0}} = [X^{O(1)}_{FR02}]$	$X^{O(1)}_{FR02}$	Natural diet	Null		

another successor, keep lengthen the chain toward another direction, and if not, this new last design resource should also be removed.

Step 6. Keep on doing Step 3–5, so that the generated design resource chain could be lengthened and shortened in turn, and finally, it becomes empty again.

Step 7. If there are still other starting design resources in the design resource graph, add one of them into the generated design resource chain as the 1st design resource and repeat Step 2–6.

Step 8. Keep on doing Step 7, until there is no other starting design resource rest.

These algorithm steps are concluded into a flow diagram shown in Figure 6.

To illustrate the above algorithm in detailed case, here take the design resource graph shown in Figure 4 as an example. Assume that DR1 and DR3 are the starting design resources, and DR17 is the ending design resource. Set the limitation of the generated design resource chain's length as 6 DRs. The operating steps of the algorithm and the corresponding changes of the generated design resource chain are shown in Table 2, and the operating steps are also shown in Figure 7 for a visual representation.

Mapping from the functional domain to the physical domain

With the above proposed design parameter classification, design resource graph, design resource chain generating algorithm, and design resource combination construction, a systematical transformation from the functional requirements to the design parameters is formed within the distributed design resource environment as shown in Figure 8.

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

Table 5. Detailed information of FR011, FR012, FR013, FR021, and FR022

Functional requirement	Input and output vectors		Inputs and outputs			
			Name	Features		
				Name	Value range	Unit
FR011	$\overrightarrow{X^{I}_{FR011}} = \begin{bmatrix} X^{I(1)}_{FR011} \\ X^{I(2)}_{FR011} \\ X^{I(3)}_{FR011} \\ X^{I(4)}_{FR011} \\ X^{I(5)}_{FR011} \end{bmatrix}$	$X^{I(1)}_{FR011}$	Sunlight	Illumination intensity	[60,000, 100,000]	lx
				Color temperature	[5000.0, 7000.0]	K
				Frequency	[510.0, 530.0]	Hz
				Energy density	[800.0, 1200.0]	W/m^2
		$X^{I(2)}_{FR011}$	River flow	Flow velocity	[0.8, 2.0]	m/s
				Flow rate	[0.65, 1.87]	m^3/s
		$X^{I(3)}_{FR011}$	Daily garbage	Water content	[15.0, 85.0]	%
				Particle diameter	[0.5, 800.0]	mm
		$X^{I(4)}_{FR011}$	Maize straw	Density	[800.0, 1400.0]	kg/m^3
				Ash content	[1.0, 10.0]	%
				Water content	[2.0, 15.0]	%
				Caloricity	[3700.0, 5000.0]	kcal
		$X^{I(5)}_{FR011}$	Organic food	Null		
	$\overrightarrow{X^{O}_{FR011}} = [X^{O(1)}_{FR011}]$	$X^{O(1)}_{FR011}$	Natural illumination	Illumination intensity	[30, 300]	lx
				Color temperature	[3500.0, 5000.0]	K
FR012	$\overrightarrow{X^{I}_{FR012}} = \begin{bmatrix} X^{I(1)}_{FR012} \\ X^{I(2)}_{FR012} \\ X^{I(3)}_{FR012} \\ X^{I(4)}_{FR012} \\ X^{I(5)}_{FR012} \end{bmatrix}$	$X^{I(1)}_{FR012}$	Sunlight	Illumination intensity	[60,000, 100,000]	lx
				Color temperature	[5000.0, 7000.0]	K
				Frequency	[510.0, 530.0]	Hz
				Energy density	[800.0, 1200.0]	W/m^2
		$X^{I(2)}_{FR012}$	River flow	Flow velocity	[0.8, 2.0]	m/s
				Flow rate	[0.65, 1.87]	m^3/s
		$X^{I(3)}_{FR012}$	Daily garbage	Water content	[15.0, 85.0]	%
				Particle diameter	[0.5, 800.0]	mm
		$X^{I(4)}_{FR012}$	Maize straw	Density	[800.0, 1400.0]	kg/m^3
				Ash content	[1.0, 10.0]	%
				Water content	[2.0, 15.0]	%
				Caloricity	[3700.0, 5000.0]	kcal
		$X^{I(5)}_{FR012}$	Organic food	Null		
	$\overrightarrow{X^{O}_{FR012}} = [X^{O(1)}_{FR012}]$	$X^{O(1)}_{FR012}$	Heating	Thermal power	[30, 45]	W
FR013	$\overrightarrow{X^{I}_{FR013}} = \begin{bmatrix} X^{I(1)}_{FR013} \\ X^{I(2)}_{FR013} \\ X^{I(3)}_{FR013} \\ X^{I(4)}_{FR013} \\ X^{I(5)}_{FR013} \end{bmatrix}$	$X^{I(1)}_{FR013}$	Sunlight	Illumination intensity	[60,000, 100,000]	lx
				Color temperature	[5000.0, 7000.0]	K
				Frequency	[510.0, 530.0]	Hz
				Energy density	[800.0, 1200.0]	W/m^2
		$X^{I(2)}_{FR013}$	River flow	Flow velocity	[0.8, 2.0]	m/s
				Flow rate	[0.65, 1.87]	m^3/s
		$X^{I(3)}_{FR013}$	Daily garbage	Water content	[15.0, 85.0]	%
				Particle diameter	[0.5, 800.0]	mm
		$X^{I(4)}_{FR013}$	Maize straw	Density	[800.0, 1400.0]	kg/m^3
				Ash content	[1.0, 10.0]	%
				Water content	[2.0, 15.0]	%

(*Continued*)

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

Table 5. (*Continued.*)

Functional requirement	Input and output vectors	Inputs and outputs				
			Name	Features		
				Name	Value range	Unit
				Caloricity	[3700.0, 5000.0]	kcal
		$X_{FR013}^{I(5)}$	Organic food	Null		
	$\overrightarrow{X_{FR013}^{O}} = [X_{FR013}^{O(1)}]$	$X_{FR013}^{O(1)}$	Municipal electricity	Voltage	220	V
				Frequency	60	Hz
				Phase number	3	Null
FR021	$\overrightarrow{X_{FR021}^{I}} = \begin{bmatrix} X_{FR021}^{I(1)} \\ X_{FR021}^{I(2)} \\ X_{FR021}^{I(3)} \\ X_{FR021}^{I(4)} \\ X_{FR021}^{I(5)} \end{bmatrix}$	$X_{FR021}^{I(1)}$	Sunlight	Illumination intensity	[60,000, 100,000]	lx
				Color temperature	[5000.0, 7000.0]	K
				Frequency	[510.0, 530.0]	Hz
				Energy density	[800.0, 1200.0]	W/m^2
		$X_{FR021}^{I(2)}$	River flow	Flow velocity	[0.8, 2.0]	m/s
				Flow rate	[0.65, 1.87]	m^3/s
		$X_{FR021}^{I(3)}$	Daily garbage	Water content	[15.0, 85.0]	%
				Particle diameter	[0.5, 800.0]	mm
		$X_{FR021}^{I(4)}$	Maize straw	Density	[800.0, 1400.0]	kg/m^3
				Ash content	[1.0, 10.0]	%
				Water content	[2.0, 15.0]	%
				Caloricity	[3700.0, 5000.0]	kcal
		$X_{FR021}^{I(5)}$	Organic food	Null		
	$\overrightarrow{X_{FR021}^{O}} = [X_{FR021}^{O(1)}]$	$X_{FR021}^{O(1)}$	Fuel gas	Heating capacity	[20.0, 25.0]	MJ/m^3
FR022	$\overrightarrow{X_{FR022}^{I}} = \begin{bmatrix} X_{FR022}^{I(1)} \\ X_{FR022}^{I(2)} \\ X_{FR022}^{I(3)} \\ X_{FR022}^{I(4)} \\ X_{FR022}^{I(5)} \end{bmatrix}$	$X_{FR022}^{I(1)}$	Sunlight	Illumination intensity	[60,000, 100,000]	lx
				Color temperature	[5000.0, 7000.0]	K
				Frequency	[510.0, 530.0]	Hz
				Energy density	[800.0, 1200.0]	W/m^2
		$X_{FR022}^{I(2)}$	River flow	Flow velocity	[0.8, 2.0]	m/s
				Flow rate	[0.65, 1.87]	m^3/s
		$X_{FR022}^{I(3)}$	Daily garbage	Water content	[15.0, 85.0]	%
				Particle diameter	[0.5, 800.0]	mm
		$X_{FR022}^{I(4)}$	Maize straw	Density	[800.0, 1400.0]	kg/m^3
				Ash content	[1.0, 10.0]	%
				Water content	[2.0, 15.0]	%
				Caloricity	[3700.0, 5000.0]	kcal
		$X_{FR022}^{I(5)}$	Organic food	Null		
	$\overrightarrow{X_{FR022}^{O}} = [X_{FR022}^{O(1)}]$	$X_{FR022}^{O(1)}$	Healthy diet	Null		

As shown in Figure 8, for a functional requirement, there are three possibilities for the process of finding its proper design parameter. Firstly, current design parameters (design resource combinations or design resources) can be analyzed, if there is any design resource feature can achieve this functional requirement, this design resource feature is the proper design parameter. If there is no proper design resource feature found, the design resource chain generating algorithm should be executed by the computer within the design resource graph, so that the design resource or design resource combination can be generated to achieve the functional requirement. At this time, this design resource or design resource combination is the proper design parameter. But, if there is still no proper design resource or design resource combination found, the zigg-zagging should be kept on, which means this functional requirement should be decomposed just as mentioned in the traditional AD theory. The whole process

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

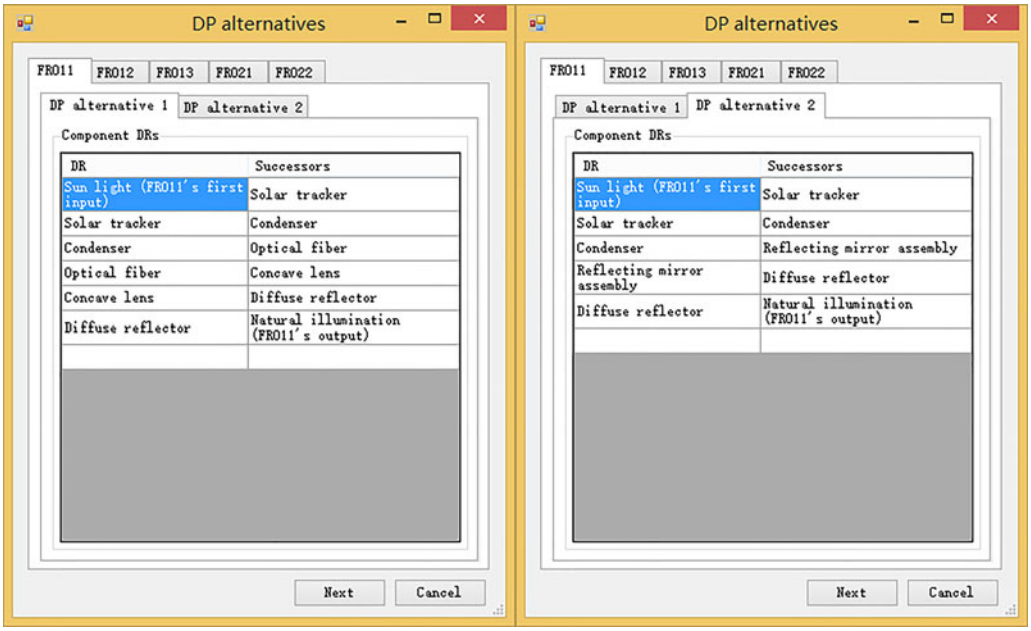


Fig. 13. Alternative design parameters for FR011.

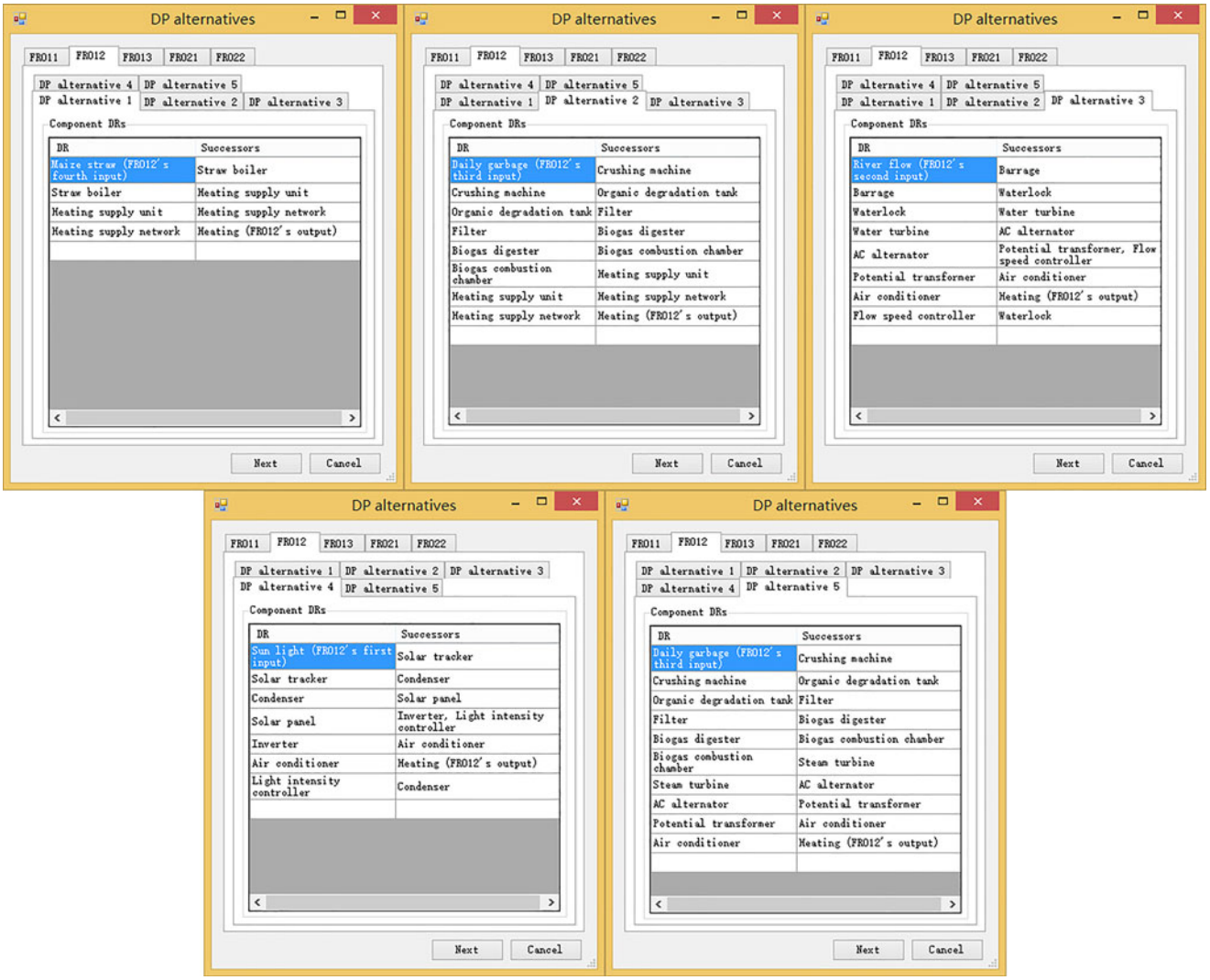


Fig. 14. Alternative design parameters for FR012.

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

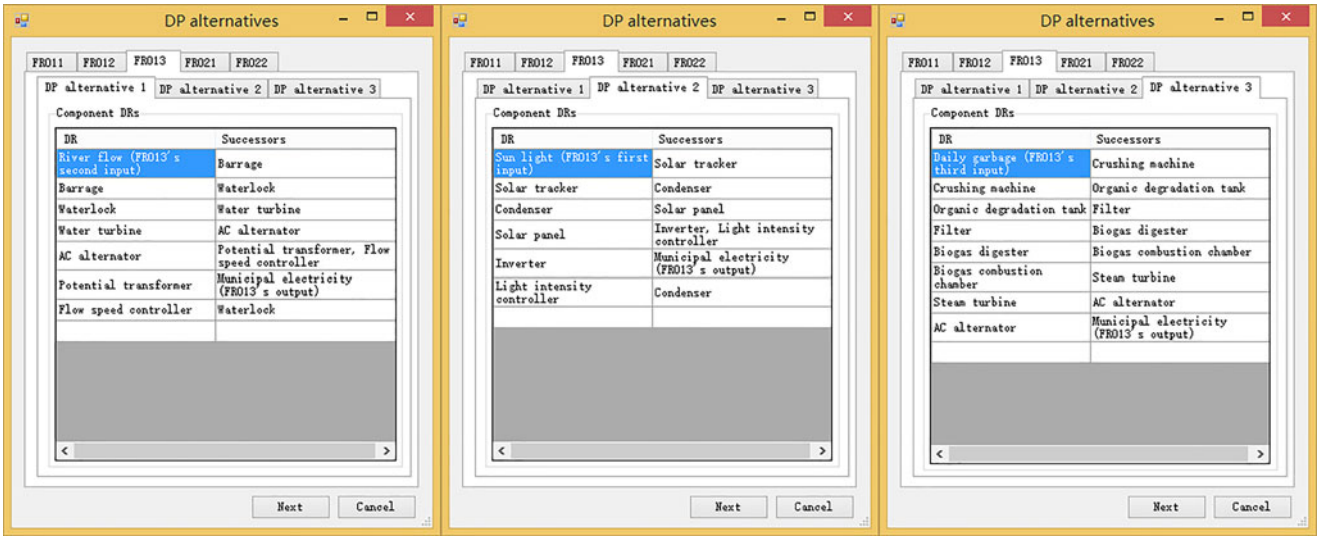


Fig. 15. Alternative design parameters for FR013.

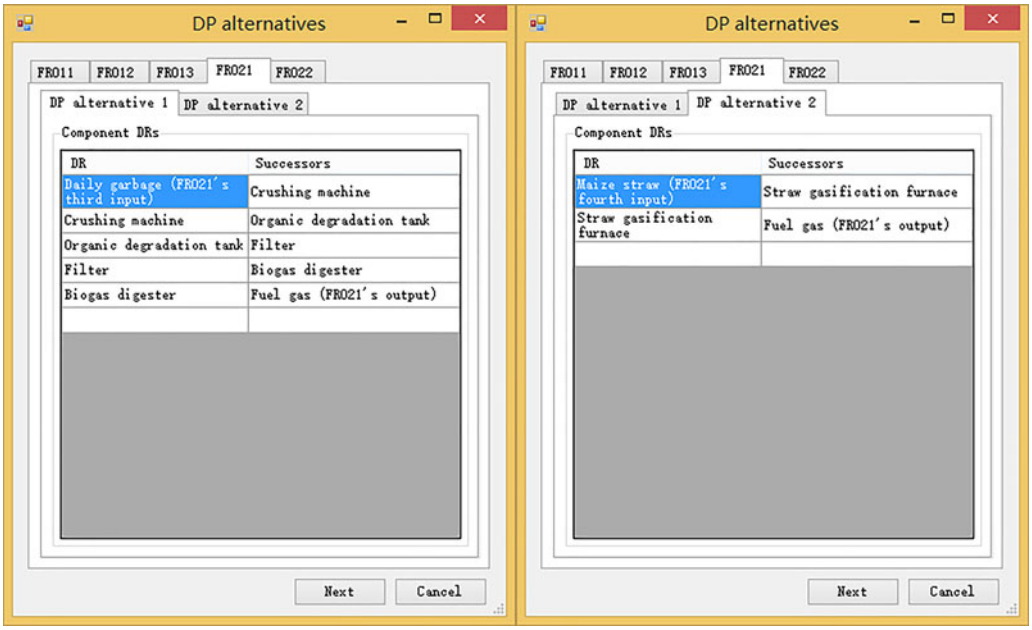


Fig. 16. Alternative design parameters for FR021.

now can be concluded as a computer-aided approach for the mapping from the functional domain to the physical domain as shown in Figure 9.

During the zigg-zagging, the design equations in all the levels should be written down, and the design matrices should be checked with the independence axiom, so that the coupled relationship between functional requirements and design parameters can be avoided. Here, in this case, if this mapping meets the independence axiom, its design equations should be as follows:

$$\text{Level 1: FR} = [X]\text{DP}, \tag{41}$$

$$\text{Level 2: } \begin{bmatrix} \text{FR1} \\ \text{FR2} \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} \text{DP1} \\ \text{DP2} \end{bmatrix}, \tag{42}$$

$$\text{Level 3: } \begin{bmatrix} \text{FR11} \\ \text{FR12} \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} \text{DP11} \\ \text{DP12} \end{bmatrix}, \quad \text{FR21} = [X]\text{DP21}, \tag{43}$$

$$\text{Level 4: } \begin{bmatrix} \text{FR111} \\ \text{FR112} \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} \text{DP111} \\ \text{DP112} \end{bmatrix}, \begin{bmatrix} \text{FR121} \\ \text{FR122} \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} \text{DP121} \\ \text{DP122} \end{bmatrix}. \tag{44}$$

Now, this mapping is a feasible mapping. Additionally, if there is more than one mapping obtained, the alternatives should be tested by the information axiom, so that the optimal one can be picked out.

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

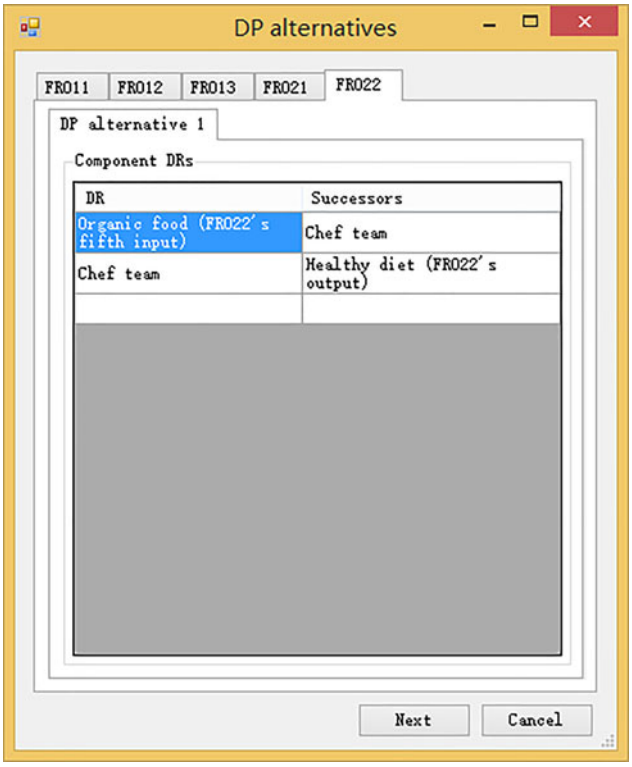


Fig. 17. Alternative design parameters for FR022.

Implementation

To prove the feasibility of this proposed computer-aided approach, a software prototype called the ADS-DDRE is established. ADS-DDRE's root database is set on several central servers, and its client part can be configured on personal computers. Design resource providers distributed in different locations, institutes, and disciplines can publish their design resources on the Internet by the client part, and the design resources' data is stored in the root database as a design resource graph. Designers can visit the root database through the client part, and complete the data processing work, including design resource searching, design resource chain generating, and design resource combination constructing, within the design resource graph by the proposed design resource chain generating algorithm. Next, a natural leisure hotel is designed by ADS-DDRE as an example.

This natural leisure hotel is aimed to take full advantages of the natural resources, like the sunlight, the river flow, the daily garbage, the maize straw, and the organic food, to supply natural leisure services for the customers. This functional requirement can be expressed as FR0 shown in Table 3.

After figure out the functional requirement, FR0, the designers should start ADS-DDRE's client part and input FR0 as shown in Figure 10. Then, the features of FR0's inputs and output should be edited as shown in Figure 11. Click the "Next" button to start searching for FR0's design parameter. However, no proper design resource or design resource combination is found, as shown in Figure 12.

Therefore, concretize "natural leisure services" into "natural residence" and "natural diet", so that FR0 can be decomposed into FR01 and FR02 as shown in Table 4.

Now, input FR01 and FR02 into ADS-DDRE and try to find their design parameters. However, there is still no result. So, the zigg-zagging should go on, FR01 and FR02 should be further decomposed. As for FR01, to make the customers feel comfortable in the residence, this hotel should supply natural illumination, heating, and municipal electricity. So, FR01 can be decomposed into FR011, FR012, and FR013. As for FR02, the customers need a healthy diet, which comes from a professional kitchen with enough fuel gas supplement. Thus, FR02 can be decomposed into FR021 and FR022. The detailed information of FR011, FR012, FR013, FR021, and FR022 is shown in Table 5.

Input these five functional requirements into ADS-DDRE and begin to search the corresponding design parameters. This time, some alternatives can be found for each functional requirement as shown in Figures 13–17.

Based on the tables shown in Figures 13–17, the design parameter alternatives for FR011, FR012, FR013, FR021, and FR022 can be described by the intuitionistic diagrams shown in Figures 18–22.

There are many design parameter alternatives found by ADS-DDRE for the functional requirements, that is, two for FR011, five for FR012, three for FR013, two for FR021, and one for FR022. Therefore, the final design parameter for this design case should be one of the combinations of these five groups of design parameter alternatives, which meets the independence axiom and information axiom the most.

There are 60 ($2 \times 5 \times 3 \times 2 \times 1 = 60$) design parameter alternative combinations here in total. First, figure out their design matrices and test them with independence axiom.

The design equations of the 60 design parameter alternative combinations are shown in Table 6. There are 12 design parameter alternative combinations go through the independence axiom test, so all of them are decoupled.

To select the optimal one from the 12 design parameter alternative combinations, their component design resource number should be figured out, as shown in Table 7.

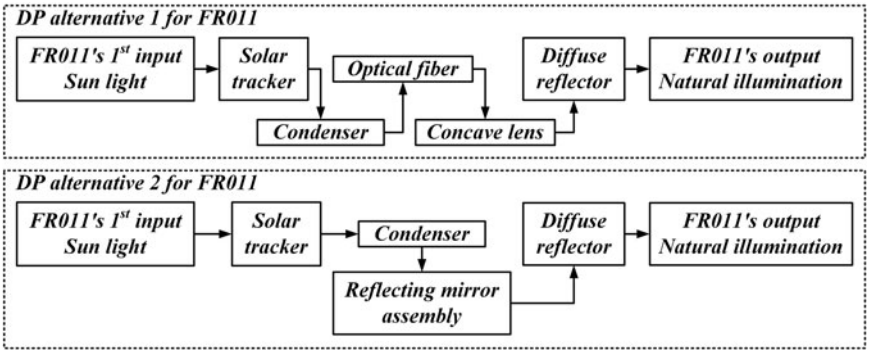


Fig. 18. Design parameter alternatives for FR011.

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

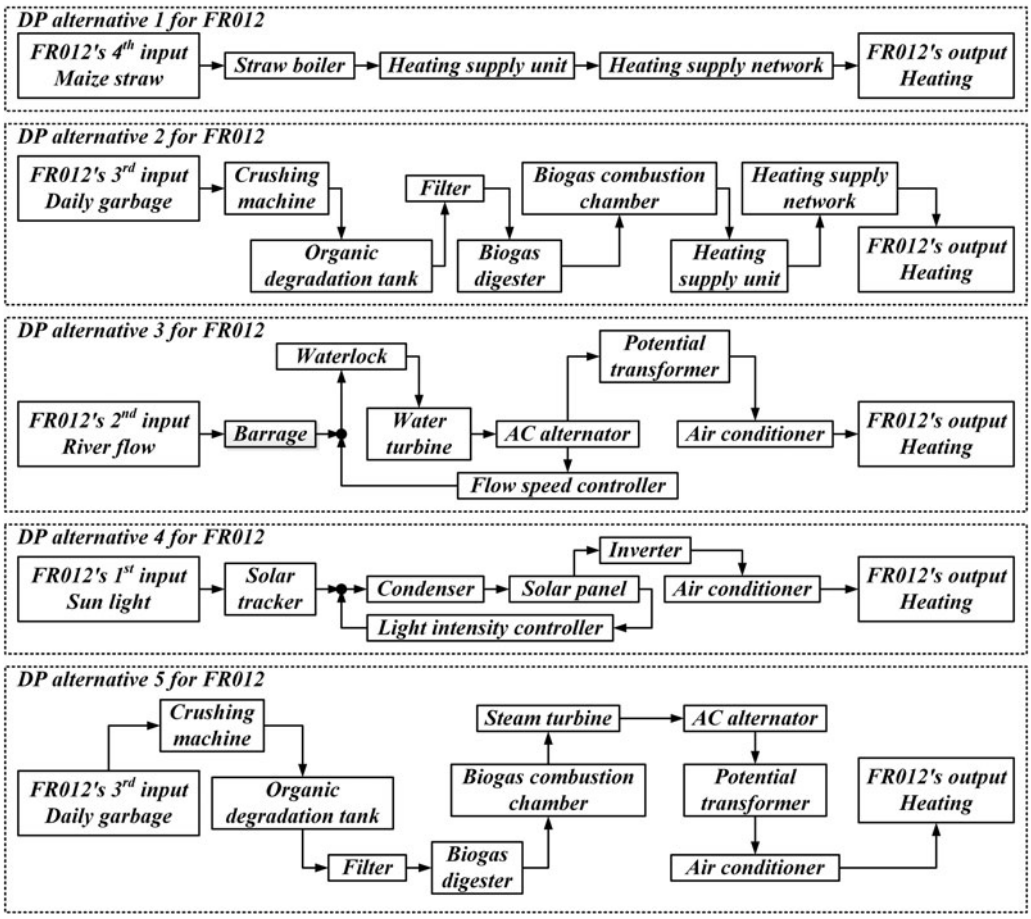


Fig. 19. Design parameter alternatives for FR012.

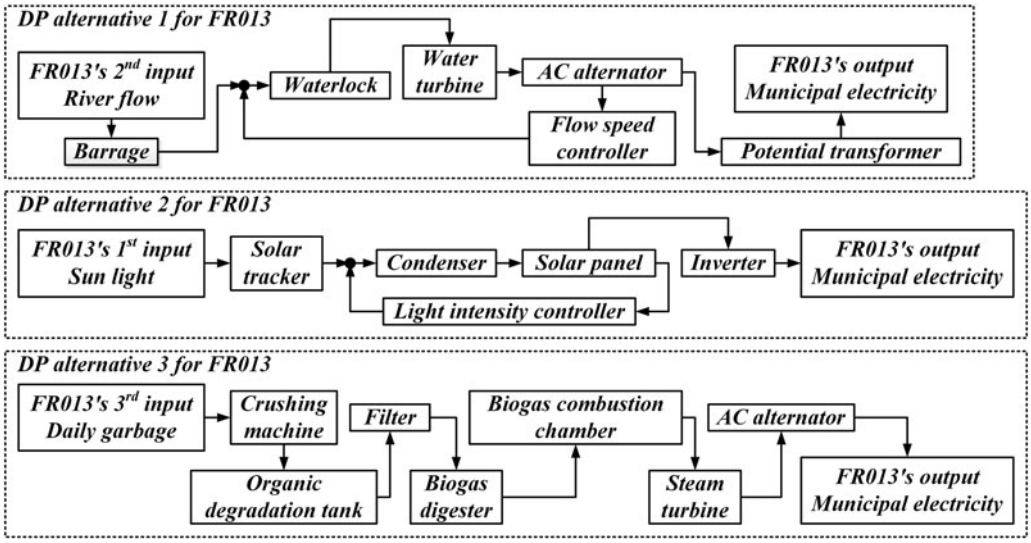


Fig. 20. Design parameter alternatives for FR013.

Here, the design parameter alternative combination, C32, consists of the least design resources, which means it contains the least information. Based on the information axiom, here should take C32 as the optimal design scheme as shown in Figure 23. In this design solution, there are five design parameters in total, that is, DP011 for FR011, DP012 for FR012, DP013 for FR013,

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

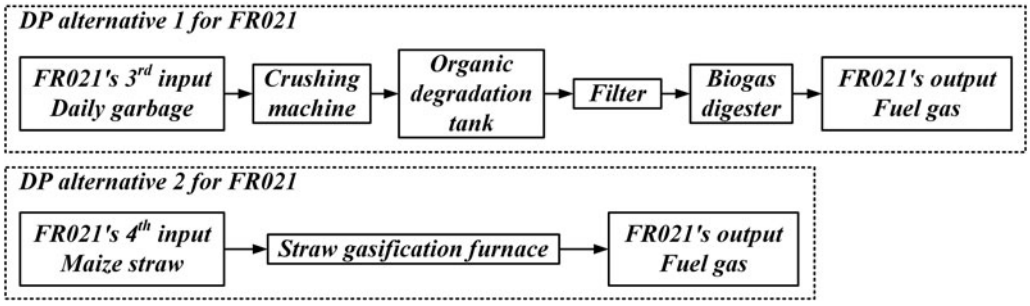


Fig. 21. Design parameter alternatives for FR021.

DP021 for FR021, and DP022 for FR022. Among them, DP021 and DP022 are design resources, and DP011, DP012, and DP013 are design resource combinations.

Discussion

Compared with other AD methods, this proposed approach has two unique advantages:

(1) This approach is constructed on a classification of design parameters proposed in this study. In the former researches, the classification of design parameters is not paid enough attention to. With a good classification, the constructive granularities of the design parameters can be distinguished, so that their constructing process can be subtly analyzed, decomposed, and finally computerized into an executable algorithm. Furthermore, this classification can also be introduced into the software design (the three kinds may correspond to software packages, modules, and features), healthcare system design, manufacturing system design, and other design missions not limited in the domain of product design. In the future works, this part of work will be carried on to contribute to AD theory.
(2) This approach automates the transformation from the functional requirement to the design parameters. In the former AD methods, there are mature tools for the decomposition of the functional requirement; however, the transformation from the functional requirement to the design parameters still largely relies on the designers' own knowledge, experience, and inspiration. The data model of distributed design resource environment, design resource graph, is proposed to offer a running space for a proposed computer-executable algorithm, which takes the data processing workload of design parameter obtaining.
(3) This approach introduces the distributed design resource environment into the AD theory. In the former AD methods, all the raw materials for the design mission are assumed accessible for the designers, which means a limitation of design resources is premised considering the designers' own knowledge, experience, sociality, and capability. In this approach, all the raw materials for the design mission are assumed coming from the distributed design resource environment, which consists of numerous design resources from different locations, institutes, and disciplines. So, the contradiction between the designers' increasingly innovative design conception and the limitation of their access to rich design resources and powerful computing capacity can be alleviated.

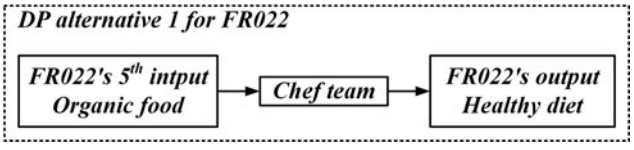


Fig. 22. Design parameter alternatives for FR022.

This approach also has limitations which still need further work.

(1) This approach may lead to a combinatorial explosion in the possibilities. The diversity of the design solution comes from two places in this study. First, the design resources used to construct the design solution come from the distributed design resource environment, which means their quantity is very large. Second, there may be many different combining structures consisting of the same group of design resources. Furthermore, as the quantity of the design resources increases, the quantity of the possible structures also grows increasingly faster. Indeed, diversity is positive for the promotion of the design innovation but that should be supported by the fitting data processing capability of the computing strategy. Therefore, in the future works, the concurrent multiprocess computing strategy will be considered as an improvement for the current algorithm because its computing resource scale can also be expanded as the increasingly growing distributed design resource environment.
(2) This approach still lacks an evaluating system for the design parameters. As mentioned above, with the distributed design resource environment, the quantity of alternative design parameters for a functional requirement may be very large. Thus, there should be an evaluating system to help the designers investigate the alternatives. In the future work, an evaluating system will be considered established to rank the design parameters based on their performances according to the design constraints, like price, weight, size, environmental protecting capability, using comfort, etc.

Conclusion

In this paper, a computer-aided approach is proposed to improve the AD theory with the distributed design resource environment.

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

Table 6. Design equations of the design parameter alternative combinations

No.	DP alternatives for the FRs					Design equations		
	FR011	FR012	FR013	FR021	FR022	FR01,FR02 and DP01,DP02	FR011,FR012,FR013 and DP011,DP012,DP013	FR021,FR022 and DP021,DP022
C1	DPA1	DPA1	DPA1	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&0\\0&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C2	DPA1	DPA1	DPA1	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&0\\0&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C3	DPA1	DPA1	DPA2	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&X\\0&X&0\\X&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C4	DPA1	DPA1	DPA2	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&X\\0&X&0\\X&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C5	DPA1	DPA1	DPA3	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&X\\X&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&0\\0&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C6	DPA1	DPA1	DPA3	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&0\\0&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C7	DPA1	DPA2	DPA1	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&X\\X&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&0\\0&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C8	DPA1	DPA2	DPA1	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&0\\0&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C9	DPA1	DPA2	DPA2	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&X\\X&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&X\\0&X&0\\X&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C10	DPA1	DPA2	DPA2	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&X\\0&X&0\\X&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C11	DPA1	DPA2	DPA3	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&X\\X&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&X\\0&X&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C12	DPA1	DPA2	DPA3	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&X\\0&X&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C13	DPA1	DPA3	DPA1	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&X\\0&X&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C14	DPA1	DPA3	DPA1	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&X\\0&X&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C15	DPA1	DPA3	DPA2	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&X\\0&X&0\\X&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C16	DPA1	DPA3	DPA2	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&X\\0&X&0\\X&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C17	DPA1	DPA3	DPA3	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&X\\X&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&0\\0&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C18	DPA1	DPA3	DPA3	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&0\\0&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C19	DPA1	DPA4	DPA1	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&X&0\\X&X&0\\0&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C20	DPA1	DPA4	DPA1	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&X&0\\X&X&0\\0&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C21	DPA1	DPA4	DPA2	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&X&X\\X&X&X\\X&X&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C22	DPA1	DPA4	DPA2	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&X&X\\X&X&X\\X&X&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C23	DPA1	DPA4	DPA3	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&X\\X&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&X&0\\X&X&0\\0&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C24	DPA1	DPA4	DPA3	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&X&0\\X&X&0\\0&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C25	DPA1	DPA5	DPA1	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&X\\X&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&0\\0&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C26	DPA1	DPA5	DPA1	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&0\\0&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C27	DPA1	DPA5	DPA2	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&X\\X&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&X\\0&X&0\\X&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C28	DPA1	DPA5	DPA2	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&X\\0&X&0\\X&0&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C29	DPA1	DPA5	DPA3	DPA1	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&X\\X&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&X\\0&X&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$
C30	DPA1	DPA5	DPA3	DPA2	DPA1	$\begin{bmatrix}FR01\\FR02\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP01\\DP02\end{bmatrix}$	$\begin{bmatrix}FR011\\FR012\\FR013\end{bmatrix}=\begin{bmatrix}X&0&0\\0&X&X\\0&X&X\end{bmatrix}\begin{bmatrix}DP011\\DP012\\DP013\end{bmatrix}$	$\begin{bmatrix}FR021\\FR022\end{bmatrix}=\begin{bmatrix}X&0\\0&X\end{bmatrix}\begin{bmatrix}DP021\\DP022\end{bmatrix}$

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

C31	DPA2	DPA1	DPA1	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & 0 \\ 0 & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C32	DPA2	DPA1	DPA1	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & 0 \\ 0 & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C33	DPA2	DPA1	DPA2	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & X \\ 0 & X & 0 \\ X & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C34	DPA2	DPA1	DPA2	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & X \\ 0 & X & 0 \\ X & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C35	DPA2	DPA1	DPA3	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & X \\ X & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & 0 \\ 0 & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C36	DPA2	DPA1	DPA3	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & 0 \\ 0 & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C37	DPA2	DPA2	DPA1	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & X \\ X & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & 0 \\ 0 & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C38	DPA2	DPA2	DPA1	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & 0 \\ 0 & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C39	DPA2	DPA2	DPA2	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & X \\ X & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & X \\ 0 & X & 0 \\ X & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C40	DPA2	DPA2	DPA2	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & X \\ 0 & X & 0 \\ X & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C41	DPA2	DPA2	DPA3	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & X \\ X & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & X \\ 0 & X & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C42	DPA2	DPA2	DPA3	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & X \\ 0 & X & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C43	DPA2	DPA3	DPA1	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & X \\ 0 & X & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C44	DPA2	DPA3	DPA1	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & X \\ 0 & X & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C45	DPA2	DPA3	DPA2	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & X \\ 0 & X & 0 \\ X & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C46	DPA2	DPA3	DPA2	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & X \\ 0 & X & 0 \\ X & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C47	DPA2	DPA3	DPA3	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & X \\ X & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & 0 \\ 0 & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C48	DPA2	DPA3	DPA3	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & 0 \\ 0 & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C49	DPA2	DPA4	DPA1	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & X & 0 \\ X & X & 0 \\ 0 & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C50	DPA2	DPA4	DPA1	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & X & 0 \\ X & X & 0 \\ 0 & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C51	DPA2	DPA4	DPA2	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & X & X \\ X & X & X \\ X & X & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C52	DPA2	DPA4	DPA2	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & X & X \\ X & X & X \\ X & X & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C53	DPA2	DPA4	DPA3	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & X \\ X & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & X & 0 \\ X & X & 0 \\ 0 & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C54	DPA2	DPA4	DPA3	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & X & 0 \\ X & X & 0 \\ 0 & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C55	DPA2	DPA5	DPA1	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & X \\ X & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & 0 \\ 0 & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C56	DPA2	DPA5	DPA1	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & 0 \\ 0 & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C57	DPA2	DPA5	DPA2	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & X \\ X & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & X \\ 0 & X & 0 \\ X & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C58	DPA2	DPA5	DPA2	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & X \\ 0 & X & 0 \\ X & 0 & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C59	DPA2	DPA5	DPA3	DPA1	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & X \\ X & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & X \\ 0 & X & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$
C60	DPA2	DPA5	DPA3	DPA2	DPA1	$\begin{bmatrix} FR01 \\ FR02 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP01 \\ DP02 \end{bmatrix}$	$\begin{bmatrix} FR011 \\ FR012 \\ FR013 \end{bmatrix} = \begin{bmatrix} X & 0 & 0 \\ 0 & X & X \\ 0 & X & X \end{bmatrix} \begin{bmatrix} DP011 \\ DP012 \\ DP013 \end{bmatrix}$	$\begin{bmatrix} FR021 \\ FR022 \end{bmatrix} = \begin{bmatrix} X & 0 \\ 0 & X \end{bmatrix} \begin{bmatrix} DP021 \\ DP022 \end{bmatrix}$

"DPA" is short for "Design parameter alternative".

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

Table 7. Design resource number of the 12 design parameter alternative combinations

DPA Combination	FR011	FR012	FR013	FR021	FR022	DR number
C1	DPA1	DPA1	DPA1	DPA1	DPA1	19
C2	DPA1	DPA1	DPA1	DPA2	DPA1	16
C6	DPA1	DPA1	DPA3	DPA2	DPA1	17
C8	DPA1	DPA2	DPA1	DPA2	DPA1	20
C18	DPA1	DPA3	DPA3	DPA2	DPA1	21
C26	DPA1	DPA5	DPA1	DPA2	DPA1	22
C31	DPA2	DPA1	DPA1	DPA1	DPA1	18
C32	**DPA2**	**DPA1**	**DPA1**	**DPA2**	**DPA1**	**15**
C36	DPA2	DPA1	DPA3	DPA2	DPA1	16
C38	DPA2	DPA2	DPA1	DPA2	DPA1	19
C48	DPA2	DPA3	DPA3	DPA2	DPA1	20
C56	DPA2	DPA5	DPA1	DPA2	DPA1	21

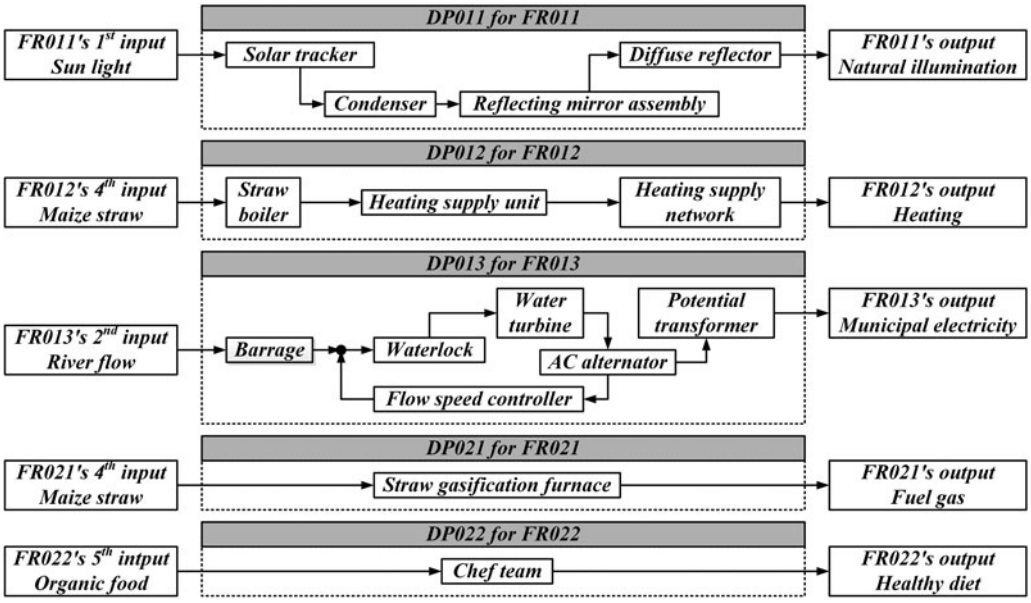


Fig. 23. Final design solution.

It is aimed to help designers with the mapping from the functional domain to the physical domain. A classification is proposed to distinguish the constructive granularities of the design parameters into three levels, that is, design resource, design resource feature, and design resource combination. Therefore, a systematical transformation from the functional requirement to the design parameter is constructed with a computer-executable algorithm, which searches and combines the design resources in the design resource graph (a data model proposed for the distributed design resource environment). This systematical transformation is embedded into the zigg-zagging, so that a computer-aided approach is formed for the mapping from the functional domain to the physical domain. Finally, to prove the feasibility of this proposed approach, a software prototype called ADS-DDRE is established, and a natural leisure hotel is designed as an implementation case.

Funding. This research is supported by the National Natural Science Foundation of China (Grant Nos. 51805322, 51775332, 51805319, and 51675329), the China Postdoctoral Science Foundation (Grant No. 2018M642008), the Major Project of National Social Science Fund, China (Grant No. 17ZDA020), the Shanghai Committee of Science and Technology (Grant No. 16XD1425000), and the Special Program for Innovation Method of the Ministry of Science and Technology, China (Grant No. 2018IM020100).

References

Camelo DM and Mulet E (2010) A multi-relational and interactive model for supporting the design process in the conceptual phase. *Automation in Construction* **19**, 964–974.

Chakrabarti A and Bligh TP (2001) A scheme for functional reasoning in conceptual design. *Design Studies* **22**, 493–517.

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press

Chen B and Xie Y (2017*a*) Functional knowledge integration of the design process. *Science China Technological Sciences* **60**, 209–218.

Chen B and Xie YB (2017*b*) A computer-assisted automatic conceptual design system for the distributed multi-disciplinary resource environment. *Proceedings of the Institution of Mechanical Engineers, Part C: Journal of Mechanical Engineering Science* **231**, 1094–1112

Chen X, Li Z, Fan ZP, Zhou X and Zhang X (2016) Matching demanders and suppliers in knowledge service: a method based on fuzzy axiomatic design. *Information Sciences* **346**, 130–145

Chen W, Goh M and Zou Y (2018) Logistics provider selection for omni-channel environment with fuzzy axiomatic design and extended regret theory. *Applied Soft Computing* **71**, 353–363.

Cheng J, Feng Y, Lin Z, Liu Z and Tan J (2017) Anti-vibration optimization of the key components in a turbo-generator based on heterogeneous axiomatic design. *Journal of Cleaner Production* **141**, 1467–1477.

Cochran DS, Arinez JF, Duda JW and Linck J (2001) A decomposition approach for manufacturing system design. *Journal of Manufacturing Systems* **20**, 371–389.

Cochran DS, Hendricks S, Barnes J and Bi Z (2016) Extension of manufacturing system design decomposition to implement manufacturing systems that are sustainable. *Journal of Manufacturing Science and Engineering* **138**, 101006.

Cochran DS, Foley JT and Bi Z (2017) Use of the manufacturing system design decomposition for comparative analysis and effective design of production systems. *International Journal of Production Research* **55**, 870–890.

Deo HV and Suh NP (2004) Mathematical transforms in design: case study on feedback control of a customizable automotive suspension. *CIRP Annals-Manufacturing Technology* **53**, 125–128

Drakaki M, Gören HG and Tzionas P (2018) An intelligent multi-agent system using fuzzy analytic hierarchy process and Axiomatic Design as a decision support method for refugee settlement siting. In Dargam F, Delias P, Linden I and Mareschal B (eds), *Decision Support Systems VIII Sustainable Data-Driven and Evidence-Based Decision Support. ICDSST 2018*, Vol.**313**. Cham: Springer, pp. 15–25, Lecture Notes in Business Information Processing.

Gualtieri L, Rauch E, Rojas R, Vidoni R and Matt DT (2018) Application of Axiomatic Design for the design of a safe collaborative human-robot assembly workplace. *MATEC Web of Conferences* 223, 01003.

He B, Niu Y, Hou S and Li F (2018) Sustainable design from functional domain to physical domain. *Journal of Cleaner Production* **197**, 1296–1306.

Helms B and Shea K (2012) Computational synthesis of product architectures based on object-oriented graph grammars. *Journal of Mechanical Design* **134**, 021008.

Hirtz J, Stone RB, Mcadams DA, Szykman S and Wood KL (2002) A functional basis for engineering design: reconciling and evolving previous efforts. *Research in Engineering Design* **13**, 65–82.

Joskowicz L and Neville D (1996) A representation language for mechanical behavior. *Artificial Intelligence in Engineering* **10**, 109–116.

Li W, Song Z, Mao E and Suh S (2019) Using Extenics to describe coupled solutions in Axiomatic Design. *Journal of Engineering Design* **30**, 1–31

Muenzer C and Shea K (2015) A simulation-based CDS approach: automated generation of simulation models based from generated concept model graphs. *Proc. ASME 2015 Int. Design Engineering Technical Conf., Computers and Information in Engineering Conf.* New York: ASME, p. V007T06A016.

Münzer C, Helms B and Shea K (2013) Automatically transforming object-oriented graph-based representations into Boolean satisfiability problems for computational design synthesis. *Journal of Mechanical Design* **135**, 101001.

Nagel RL, Perry KL, Stone RB and McAdams DA (2009) FunctionCAD: a functional modeling application based on the function design framework. *Proc. ASME 2009 Int. Design Engineering Technical Conf. /Computers and Information in Engineering Conf.* New York: ASME, pp. 591–600.

Palleti VR, Joseph JV and Silva A (2018) A contribution of axiomatic design principles to the analysis and impact of attacks on critical infrastructures. *International Journal of Critical Infrastructure Protection* **23**, 21–32.

Rauch E, Matt DT and Dallasega P (2016) Application of axiomatic design in manufacturing system design: a literature review. *Procedia CIRP* **53**, 1–7

Rauch E, Vickery A, Garcia M, Rojas R and Matt DT (2018) Axiomatic Design based design of a software prototype for smart shopfloor management. *MATEC Web of Conferences* 223, 01012.

Rauch E, Morandell F and Matt DT (2019*a*) AD design guidelines for implementing I4. 0 learning factories. *Procedia Manufacturing* **31**, 239–244.

Rauch E, Spena PR and Matt DT (2019*b*) Axiomatic design guidelines for the design of flexible and agile manufacturing and assembly systems for SMEs. *International Journal on Interactive Design and Manufacturing* **13**, 1–22.

Stone RB and Wood KL (2000) Development of a functional basis for design. *Journal of Mechanical Design* **122**, 359–370.

Stone RB, Wood KL and Crawford RH (2000) A heuristic method for identifying modules for product architectures. *Design Studies* **21**, 5–31.

Suh NP (1995) Designing-in of quality through axiomatic design. *IEEE Transactions on Reliability* **44**, 256–264.

Suh NP (2001) *Axiomatic Design: Advances and Applications*. New York: Oxford University Press.

Suh NP and Do SH (2000) Axiomatic design of software systems. *CIRP Annals-Manufacturing Technology* **49**, 95–100.

Suh NP, Cochran DS and Lima PC (1998) Manufacturing system design. *CIRP Annals-Manufacturing Technology* **47**, 627–639.

Thielman J and Ge P (2006) Applying axiomatic design theory to the evaluation and optimization of large-scale engineering systems. *Journal of Engineering Design* **17**, 1–16.

Vermaas PE and Dorst K (2007) On the conceptual framework of John Gero's FBS-model and the prescriptive aims of design methodology. *Design Studies* **28**, 133–157.

Welch RV and Dixon JR (1994) Guiding conceptual design through behavioral reasoning. *Research in Engineering Design* **6**, 169–188.

Xiao R and Cheng X (2006) Study on unifying axiomatic design and robust design. *Proceedings of the 7th International Conference on Frontiers of Design and Manufacturing (ICFDM 2006)*. Guangzhou, China, June 19–22, 2006, pp. 189–194.

Yuan L, Liu Y, Sun Z, Cao Y and Qamar A (2016) A hybrid approach for the automation of functional decomposition in conceptual design. *Journal of Engineering Design* **27**, 333–360.

Bin Chen is an Assistant Researcher in the School of Mechanical Engineering, Shanghai Jiao Tong University. Dr Chen is in charge of several research projects funded by the National Natural Science Foundation of China and the China Postdoctoral Science Foundation. His current research interests include concurrent and AI-based design in the distributed resource environment and the design theory for robots.

Jie Hu is a Professor and Executive Dean of the School of Design, Shanghai Jiao Tong University. He previously received his PhD degree from Zhejiang University and worked at Tsinghua University for postdoctoral research. Dr Hu is leading several research projects supported by the National Natural Science Foundation of China, the National Social Science Fund of China, the Ministry of Science and Technology of China, and the Shanghai Committee of Science and Technology. His research focuses on artificial intelligence in engineering design, such as conceptual design, knowledge-based design, and biologically inspired design.

Jin Qi is an Assistant Professor in the School of Mechanical Engineering, Shanghai Jiao Tong University. His research interests include case-based design and knowledge-based design. Dr Qi is in charge of several research projects funded by the National Natural Science Foundation of China and the Natural Science Foundation of Shanghai.

Weixing Chen is an Assistant Professor in the School of Mechanical Engineering, Shanghai Jiao Tong University. His research interests include ocean renewable energy and robotics. Dr Chen is in charge of several research projects funded by the National Natural Science Foundation of China and the China Postdoctoral Science Foundation.

https://doi.org/10.1017/S0890060419000283 Published online by Cambridge University Press