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A goal-directed implementation of query answering for hybrid MKNF knowledge bases

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Abstract

Ontologies and rules are usually loosely coupled in knowledge representation formalisms. In fact, ontologies use open-world reasoning, while the leading semantics for rules use non-monotonic, closed-world reasoning. One exception is the tightly coupled framework of Minimal Knowledge and Negation as Failure (MKNF), which allows statements about individuals to be jointly derived via entailment from ontology and inferences from rules. Nonetheless, the practical usefulness of MKNF has not always been clear, although recent work has formalized a general resolution-based method for querying MKNF when rules are taken to have the well-founded semantics, and the ontology is modeled by a general oracle. That work leaves open what algorithms should be used to relate the entailments of the ontology and the inferences of rules. In this paper we provide such algorithms, and describe the implementation of a query-driven system, *CDF-Rules*, for hybrid knowledge bases combining both (non-monotonic) rules under the well-founded semantics and a (monotonic) ontology, represented by the Coherent Description Framework Type-1 ($\mathscr{ALC}2$) theory.

KEYWORDS: knowledge representation, well-founded semantics, description logics, implementation

1 Introduction

Ontologies and rules offer distinctive strengths for the representation and transmission of knowledge over the Semantic Web. Ontologies offer the deductive advantages of first-order logics with an open domain while guaranteeing decidability. Rules employ non-monotonic (closed-world) reasoning that can formalize scenarios under locally incomplete knowledge; rules also offer the ability to reason about fixed points (e.g. reachability) which cannot be expressed within first-order logic.

Example 1
Consider a scenario application for a Customs Agency where an ontology is used to assess and classify aspects of imports and exports. An ontology with such characteristics would embrace several thousand axioms. In these axioms, as an

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example, one can define several axioms about countries (e.g. Scandinavian countries are European countries; Norway is a Scandinavian country; etc). Moreover, one can also model in the ontology the knowledge that is certain in the sense that it does not allow for exception. With such certain knowledge, first-order logics deduction is what is desired. For example, in this scenario, one could state that Scandinavian countries are always considered safe countries. All of this can be easily represented by an ontology defined in a Description Logic (DL) language (Baader *et al.* 2007)[1] (1),

$$\begin{aligned} &ScandinavianCountry \sqsubseteq EuropeanCountry \\ &Norway : ScandinavianCountry \\ &ScandinavianCountry \sqsubseteq SafeCountry \end{aligned} \tag{1}$$

Besides these axioms about countries, one may want to specify some additional knowledge, e.g. for defining conditions about whether or not to inspect entering shipments based on their country of origin. For example, we may want to state that one should inspect any vessel containing a shipment coming from a country that is not guaranteed to be safe. Note here that the closed world assumption is needed to define such a statement. In fact, intuitively one wants to assume that if one is unsure whether the given country is safe, then (at least for the sake of this statement) the country should be considered unsafe and an inspection performed. When using description logic with classical negation, this behavior would not be obtained, as the condition $\neg SafeCountry(country)$ would only be true in case one knows for sure that the country is not safe. However, this statement can be easily expressed by using a (non-monotonic) rule with default negation[2] as in (2),

$$inspect(X) \leftarrow hasShipment(X, Country), \mathbf{not}\ safeCountry(Country). \tag{2}$$

Such rules are non-monotonic in the sense that further knowledge – in this case about the safety of countries – can invalidate previous conclusions about inspection. This kind of non-monotonic rule is quite useful to specify default knowledge that may be subjected to exceptions. In this sense rule (2) can be seen as stating that by default shipments should be inspected, but an exception to this default rule are shipments coming from safe countries.

Note that defining some statements about a predicate using default rules does not necessarily mean that *all* statements defining that predicate should be default rules. For example, we may want to state that diplomatic shipments are not subject to inspection, regardless their country of origin. Here no default reasoning is involved. Moreover, negation here is not the default negation of logic programming, but rather classical negation. Such a statement could be modeled using normal logic programs

[1] We write DL formulas with the usual notation and the usual DL operators (see Baader *et al.* 2007) so that the argument variable of a unary predicate is not displayed and the first letter of the predicate's name is capitalized.

[2] We write rules in the usual notation for logic programming, where predicate names are non-capitalized (even if common to the ontology where they are capitalized), and variables are capitalized and implicitly universally quantified in the rule head.

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extended with explicit negation (Gelfond and Lifschitz 1990) with the rule:

$$\neg inspect(X) \leftarrow diplomaticShipment(X) \tag{3}$$

or, having the possibility to use an ontology formalized as a fragment of first-order logic, with a statement:

$$DiplomaticShipment \sqsubseteq \neg Inspect \tag{4}$$

However, these two representations of the above statement are not equivalent. In particular, with axiom 4 one can conclude that a given shipment is not diplomatic whenever one knows, by some other rule, that it should be inspected; this is not the case with rule 3. The behavior of rules with explicit negation can be easily modeled by using ontologies; for that it suffices to create a new concept standing for the explicit negation, say *NonInspect*, replacing the explicitly negated literal in the rule by this new concept, and adding the axiom $NonInspect \equiv \neg Inspect$. On the contrary, with programs extended with explicit negation one cannot obtain the full expressivity that is obtained with some of the DL-based languages for ontologies, simply because some of these languages belong to a higher complexity class. Another important feature not supported by explicit negation but typically supported by DL-based ontologies is the possibility of using existential quantification as illustrated in Example 2.

The foregoing example briefly illustrates some advantages of combining features of ontologies with features of logic programming-like rules, and of doing so in a way that allows knowledge about instances to be fully inter-definable between rules and an ontology (as happens with the predicate *inspect*/1 above, which is both defined in the rules and the ontology).

In fact, this combination of ontology and rule languages has gained particular importance in the context of the Semantic Web (Horrocks *et al.* 2006). In this context, a family of languages for representing background knowledge in the Web, OWL 2 (Hitzler *et al.* 2009), has been recommended by the World Wide Web Consortium (W3C). OWL 2 languages are based on description logics (Baader *et al.* 2007), which, as in the example above, employ open-world assumption. In addition, the rule interchange language (RIF) (Morgenstern *et al.* 2010) has recently been formally recommended to the W3C. Rule interchange language has many similarities with the logic programming language used in the above example, and adopts a closed-world assumption.

The existence of both rules and ontology languages should make it possible to combine open and closed world reasoning, and this combination is indeed important in several domains related to the Semantic Web. As a further example where this combination is desired, consider the large case study described in Patel *et al.* (2007), containing millions of assertions concerning matching patient records to clinical trials criteria. In this case study, open world reasoning is needed in deductions about domains such as radiology and laboratory data: unless a lab or radiology test asserts a negative finding, no arbitrary assumptions about the results of the test can be made (e.g. we can only be certain that some patient does not have a specific kind of cancer

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if the corresponding test is known to have negative result). However, as observed in Patel *et al.* (2007), closed world reasoning can and should be used with pharmacy data to infer that a patient is not on a medication if this is not asserted. The work of Patel *et al.* (2007) applies only open world reasoning but claims that the usage of closed world reasoning in pharmacy data would be highly desirable. Similar situations occur, for example, in matchmaking using Semantic Web Services (cf. Grimm and Hitzler 2007), where again a combination of ontology languages relying on open-world reasoning, with rule languages relying on closed-world reasoning is considered highly desirable.

Several factors influence the decision of how to combine rules and ontologies into a hybrid knowledge base. The choice of semantics for the rules, such as the answer-set semantics (Gelfond and Lifschitz 1990) or the well-founded semantics (WFS) (van Gelder *et al.* 1991), can greatly affect the behavior of the knowledge base system. The answer-set semantics offers several advantages: for instance, description logics can be translated into the answer-set semantics providing a solid basis for combining the two paradigms (Baral 2002; Eiter *et al.* 2004a; Swift 2004; Motik 2006). On the other hand, the well-founded semantics is weaker than the answer-set semantics (in the sense that it is more skeptical), but has the advantages of lower complexity and its ability to be evaluated in a query-oriented fashion, which has led to its integration into Prolog systems. Another possibility of maintaining the complexity under reasonable bounds for Semantic Web applications is to limit the expressivity of both the ontological part of the knowledge base and the rules. For instance, Calì *et al.* (2012) consider variants of Datalog that allow for existential quantification in rule heads along with other features to support a restricted form of ontological reasoning, yet restrict the rule syntax to obtain tractability.

Keeping to the general form of logic programming rules, but maintaining the complexity of reasoning under reasonable bounds, several formalisms have concerned themselves with combining ontologies with general WFS rules (Eiter *et al.* 2004b; Drabent and Małuszynski 2007; Knorr *et al.* 2008). Among these, the Well-Founded Semantics for Hybrid Minimal Knowledge and Negation as Failure (MKNF) knowledge bases ($MKNF_{WFS}$), introduced in Knorr *et al.* (2008) and viewed in Section 2, is the only one that allows knowledge about instances to be fully interdefinable between rules and an ontology that is taken as a parameter of formalism. $MKNF_{WFS}$ assigns a well-founded semantics to hybrid MKNF knowledge bases, is sound with respect to the original semantics of Motik and Rosati (2007) and, as in Motik and Rosati (2007), allows the knowledge base to have both closed- and open-world (classical) negation. For comparisons of $MKNF_{WFS}$ with the approaches for combining rules with the above-mentioned ontologies, see Knorr *et al.* (2011).

Example 2

The following fragment, adapted from an example in Motik and Rosati (2007), concerning car insurance premiums illustrates several properties of $MKNF_{WFS}$. The ontology consists of the following axioms, which state that *Married* and *NonMarried* are complementary concepts that anyone who is not married is high risk, and anyone

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with a spouse is married:

$$NonMarried \equiv \neg Married$$
$$\neg Married \sqsubseteq HighRisk$$
$$\exists Spouse.\top \sqsubseteq Married.$$

The rule base consists of the following rules, which state that anyone who is not known to be married is assumed to be non-married, those who are known to be high-risk should have a surcharge, and those that have a known spouse should have a discount:

$$\mathbf{K}\ nonMarried(X) \leftarrow \mathbf{K}\ person(X), \mathbf{not}\ married(X).$$
$$\mathbf{K}\ surcharge(X) \leftarrow \mathbf{K}\ highRisk(X), \mathbf{K}\ person(X).$$
$$\mathbf{K}\ discount(X) \leftarrow \mathbf{K}\ spouse(X, Y), \mathbf{K}\ person(X), \mathbf{K}\ person(Y).$$

Note that *married* and *nonMarried* are defined both by axioms in the ontology and by rules. Within the rule bodies, literals with the **K** or **not** operators (e.g. **K** *highRisk*(X)) may require information both from the ontology and from other rules; other literals are proven directly by the other rules (e.g. *person(X)*). Intuitively, **K**φ stands for "φ is known to be true" whereas **not** φ stands for "φ is not known to be true."

Suppose *person(john)* was added as a fact (in the rule base). Under closed-world negation, the first rule would derive *nonMarried(john)*. By the first ontology axiom, $\neg$*married(john)* would hold, and by the second axiom, *highRisk(john)* would also hold. By the last rule, *surcharge*(*john*) would hold as well. Thus, the proof of *surcharge*(*john*) involves interdependencies between the rules with closed-world negation, and the ontology with open-world negation. At the same time the proof of *surcharge*(*john*) is *relevant* in the sense that properties of other individuals, not related to *john* either through rules nor axioms in the ontology, do not need to be considered.

Now suppose that one learns that a person named Bill has a spouse, and that Bob is the spouse of Ann. This can be formalized by adding the corresponding facts for the predicate *person*, the fact *spouse*(*bob*, *ann*) and the DL assertion $bill : \exists Spouse.\top$. In this case one would expect that neither Bill nor Bob is considered high risk, and so should not have a surcharge; and since Bob (contrary to Bill) has a known spouse, he should have a discount. This is in fact the result of $MKNF_{WFS}$. Note that it is only possible to represent the difference between the situations of Bill and Bob by using the existential quantification of DL, something that is not possible in logic programming alone.

In the original definition of $MKNF_{WFS}$, the inter-dependencies of ontology and rules were captured by a bottom-up fixed-point operator with multiple levels of iterations. Recently, a query-based approach to hybrid MKNF knowledge bases, called SLG($\mathcal{O}$), has been developed using tabled resolution (Alferes *et al.* to appear). SLG($\mathcal{O}$) is sound and complete, as well as terminating for various classes of programs (e.g. datalog). In addition, SLG($\mathcal{O}$) is relevant in the sense of Example 2, i.e. in

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general, one does not need to compute the whole model (for every object in the knowledge base) to answer a specific query. This relevancy is a critical requirement for scalability in numerous practical applications (e.g. in the area of Semantic Web): Without relevance a query about a particular individual I may need to derive information about other individuals even if those individuals were not connected to I through rules or axioms. This is also clear, for example, in the above-mentioned case study about matching patient records for clinical trials criteria (Patel *et al.* 2007). In this study one is interested in finding out whether a given patient matches the criteria for a given trial or, at most, which patients match a given criteria; for scalability, it is crucial that such a query does not need to go over all patients and all criteria. In a similar manner, when assessing a shipment in Example 1, it is infeasible to consider all shipments into a country: the query must be relevant to be useful.

SLG($\mathcal{O}$) serves as a theoretical framework for query evaluation of $MKNF_{WFS}$ knowledge bases, but it models the inference mechanisms of an ontology abstractly, as an oracle. While this abstraction allows the resolution method to be parameterized by different ontology formalisms in the same manner as $MKNF_{WFS}$, it leaves open details of how ontology and rules should interact and these details must be accounted for in an implementation.

This paper in Section 4 describes the design and implementation of a prototype query evaluator[3] for $MKNF_{WFS}$, called *CDF-Rules*, which fixes the ontology part to $\mathcal{ALCQ}$ theories and makes use of the prover from XSB's ontology management library, the Coherent Description Framework (CDF) (Swift and Warren 2003) (overviewed in Section 3). To the best of our knowledge, this implementation is the first working query-driven implementation for hybrid MKNF knowledge bases, combining rules and ontology and complete with respect to the well-founded semantics.

2 MKNF well-founded semantics

Hybrid MKNF knowledge bases, as introduced in Motik and Rosati (2007), are essentially the formulas in the logics of MKNF (Lifschitz 1991), i.e. the first-order logics with equality represented as the congruence relation $\approx$, and two modal operators, **K** and **not**, which allow inspection of the knowledge base. Intuitively, given the first-order formula φ, **K** φ asks whether φ is known, while **not** φ checks whether φ is not known. A Hybrid MKNF knowledge base consists of two components: a decidable DL knowledge base, translatable into the first-order logic; and a finite set of rules of modal atoms.

Definition 1

Let $\mathcal{O}$ be a DL knowledge base built over a language $\mathcal{L}$ with distinguished sets of countably infinitely many variables N_V, along with finitely many individuals N_I,

[3] The implementation is available from the XSB CVS repository as part of the CDF package in the subdirectory `packages/altCDF/mknf`.

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and predicates (also called concepts) N_C. An atom $P(t_1,\ldots,t_n)$, where $P \in N_C$ and $t_i \in N_V \cup N_I$, is called a *DL-atom* if P occurs in $\mathcal{O}$, otherwise it is called *non-DL-atom.*

An MKNF rule r is of the form

$$\mathbf{K}\ H \leftarrow \mathbf{K}\ A_1,\ldots,\mathbf{K}\ A_n, \mathbf{not}\ B_1,\ldots,\mathbf{not}\ B_m \tag{5}$$

where H_i, A_i, and B_i are atoms. H is called the *(rule) head* and the sets $\{\mathbf{K}\ A_i\}$, and $\{\mathbf{not}\ B_j\}$ form the *(rule) body*. Atoms of the form $\mathbf{K}\ A$ are also called *positive literals* or *modal* **K**-*atoms*, while atoms of the form **not** A are called *negative literals* or *modal* **not**-*atoms.* A rule r is *positive* if $m = 0$ and a *fact* if $n = m = 0$. A *program* $\mathcal{P}$ is a finite set of MKNF rules and a *hybrid MKNF knowledge base* $\mathcal{K}$ is a pair $(\mathcal{O}, \mathcal{P})$.

In Definition 1, the modal operators of MKNF logics are only applied to atoms in the rules, which might indicate that it would suffice to use a simpler logic that does not deal with the application of the modal operators to complex formulae. However, for defining the meaning of these hybrid knowledge bases, modal operators do need to be applied to complex formulas, namely to the whole ontology $\mathcal{O}$ (cf. Definition 7). Intuitively, a hybrid knowledge base specifies that for each rule of the form (5) in $\mathcal{P}$, the atom H is known if all the A_i are known and none of the B_j is known; and that the whole ontology $\mathcal{O}$ is known (i.e. $\mathbf{K}\ \mathcal{O}$). As such, using the more general MKNF logic eases the definition of the semantics of hybrid knowledge bases, so similar to Motik and Rosati (2007) and Knorr *et al.* (2008), we resort to the full MKNF logic (Lifschitz 1991).

For decidability DL-safety is assumed, which basically constrains the use of rules to individuals actually appearing in the knowledge base under consideration. Formally, an MKNF rule r is *DL-safe* if every variable in r occurs in at least one non-DL-atom $\mathbf{K}\ B$ occurring in the body of r. A hybrid MKNF knowledge base $\mathcal{K}$ is *DL-safe* if all its rules are DL-safe (for more details we refer to Motik and Rosati 2007).

The well-founded MKNF semantics, $MKNF_{WFS}$, presented in Knorr *et al.* (2008), and further developed in Knorr *et al.* (2011), is based on a complete three-valued extension of the original MKNF semantics. However, here, as we are only interested in querying for literals and conjunctions of literals, we limit ourselves to the computation of what is called the well-founded partition in Knorr *et al.* (2008): basically the atoms that are true or false. For this reason, and in correspondence to logic programming, we name this partition the well-founded model. First, we recall some notions from Knorr *et al.* (2008), which will be useful in the definition of the operators for obtaining that well-founded model.

Definition 2

Consider a hybrid MKNF knowledge base $\mathcal{K} = (\mathcal{O}, \mathcal{P})$. The *set of* **K**-*atoms of* $\mathcal{K}$, written $\mathsf{KA}(\mathcal{K})$, is the smallest set that contains (i) all modal **K**-atoms occurring in $\mathcal{P}$, and (ii) a modal atom $\mathbf{K}\ \xi$ for each modal atom **not** ξ occurring in $\mathcal{K}$.

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Furthermore, for a set of modal atoms S, S_{DL} is the subset of DL-atoms of S (Definition 1), and $\widehat{S} = \{\xi \mid \mathbf{K}\ \xi \in S\}$.

Basically $\mathsf{KA}(\mathscr{K})$ collects all modal atoms of predicates appearing in the rules, and $\widehat{S}$ just removes $\mathbf{K}$ operators from the argument set S.

To guarantee that all atoms that are false in the ontology are also false by default in the rules, we introduce new positive DL atoms that represent the first-order false DL atoms, along with a program transformation, making these new modal atoms available for reasoning with the respective rules.

Definition 3
Let $\mathscr{K}$ be a DL-safe hybrid MKNF knowledge base. We obtain $\mathscr{K}^+$ from $\mathscr{K}$ by adding an axiom $\neg P \sqsubseteq NP$ for every DL atom P which occurs as head in at least one rule in $\mathscr{K}$, and where NP is a new predicate not already occurring in $\mathscr{K}$. Moreover, we obtain $\mathscr{K}^*$ from $\mathscr{K}^+$ by adding **not** $NP(t_1,\ldots,t_n)$ to the body of each rule with a DL atom $P(t_1,\ldots,t_n)$ in the head.

In $\mathscr{K}^+$, NP represents $\neg P$ (with its corresponding arguments) while $\mathscr{K}^*$ introduces a restriction on each rule with such a DL atom in the head, saying intuitively that the rule can only be used to conclude the head if the negation of its head cannot be proved.[4] For example, to guarantee in Example 1 that proving falsity of *Inspect* for some shipment (via the ontology) enforces default negation of *Inspect* for that shipment, one would build $\mathscr{K}^+$ by adding to the ontology the axiom $\neg Inspect \sqsubseteq N_Inspect$ (where $N_Inspect$ is a new symbol not appearing elsewhere), and in $\mathscr{K}^*$ all original rules with $inspect(X)$ in the head would be transformed by adding **not** $n_inspec(X)$ to the body. In this case, the rule in (2) would be transformed to:

$$\mathbf{K}\ inspect(X) \leftarrow \mathbf{K}\ hasShipment(X, Country), \mathbf{not}\ safeCountry(Country), \mathbf{not}\ n_inspect(X).$$

We continue by recalling the definition in Knorr *et al.* (2008) of an operator $T_{\mathscr{K}}$ to allow conclusions to be drawn from positive hybrid MKNF knowledge bases (i.e. knowledge bases where rules have no default negation).

Definition 4
For $\mathscr{K}$ a positive DL-safe hybrid MKNF knowledge base, $R_{\mathscr{K}}$, $D_{\mathscr{K}}$, and $T_{\mathscr{K}}$ are defined on subsets of $\mathsf{KA}(\mathscr{K}^*)$ as follows:

$$\begin{aligned}
R_{\mathscr{K}}(S) = S \cup \{&\mathbf{K}\ H \mid \mathscr{K} \text{ contains a rule of the form (1) such that } \mathbf{K}\ A_i \in S \\
&\text{for each } 1 \leqslant i \leqslant n\} \\
D_{\mathscr{K}}(S) = \{&\mathbf{K}\ \xi \mid \mathbf{K}\ \xi \in \mathsf{KA}(\mathscr{K}^*) \text{ and } \mathscr{O} \cup \widehat{S}_{DL} \models \xi\} \cup \{\mathbf{K}\ Q(b_1,\ldots,b_n) \mid \\
&\mathbf{K}\ Q(a_1,\ldots,a_n) \in S \setminus S_{DL},\ \mathbf{K}\ Q(b_1,\ldots,b_n) \in \mathsf{KA}(\mathscr{K}^*), \text{ and} \\
&\mathscr{O} \cup \widehat{S}_{DL} \models a_i \approx b_i \ \text{ for } 1 \leqslant i \leqslant n\} \\
T_{\mathscr{K}}(S) = R_{\mathscr{K}}(S) \cup D_{\mathscr{K}}(S)&
\end{aligned}$$

[4] Note that $\mathscr{K}^+$ and $\mathscr{K}^*$ are still hybrid MKNF knowledge bases, so we only refer to $\mathscr{K}^+$ and $\mathscr{K}^*$ explicitly when it is necessary.

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$R_{\mathscr{K}}$ derives consequences from the rules in a way similar to the classical T_P operator of definite logic programs, while $D_{\mathscr{K}}$ obtains knowledge from the ontology $\mathscr{O}$, both from non-DL-atoms and the equalities occurring in $\mathscr{O}$, where the $\approx$ operator defines a congruence relation between individuals.

The operator $T_{\mathscr{K}}$ is shown to be monotonic in Knorr *et al.* (2008), so by the Knaster–Tarski theorem, it has a unique least fixed point, denoted $\mathsf{lfp}(T_{\mathscr{K}})$, which is reached after a finite number of iteration steps.

The computation of the well-founded models follows the alternating fixed point construction (van Gelder 1989) of the well-founded semantics for logic programs. This approach requires turning a hybrid MKNF knowledge base into a positive one to make $T_{\mathscr{K}}$ applicable.

Definition 5
Let $\mathscr{K}_G = (\mathscr{O}, \mathscr{P}_G)$ be a ground DL-safe hybrid MKNF knowledge base and let $S \subseteq \mathsf{KA}(\mathscr{K}_G)$. The *MKNF transform* $\mathscr{K}_G/S = (\mathscr{O}, \mathscr{P}_G/S)$ is obtained by $\mathscr{P}_G/S$ containing all rules $\mathbf{K}\ H \leftarrow \mathbf{K}\ A_1, \ldots, \mathbf{K}\ A_n$ for which there exists a rule

$$\mathbf{K}\ H \leftarrow \mathbf{K}\ A_1, \ldots, \mathbf{K}\ A_n, \mathbf{not}\ B_1, \ldots, \mathbf{not}\ B_m$$

in $\mathscr{P}_G$ with $\mathbf{K}\ B_j \notin S$ for all $1 \leqslant j \leqslant m$.

The above transformation resembles that used for answer-sets (Gelfond and Lifschitz 1990) of logic programs and the following two operators are defined.

Definition 6
Let $\mathscr{K} = (\mathscr{O}, \mathscr{P})$ be a DL-safe hybrid MKNF knowledge base and $S \subseteq \mathsf{KA}(\mathscr{K}^*)$. We define:

$$\Gamma_{\mathscr{K}}(S) = \mathsf{lfp}(T_{\mathscr{K}^+_G/S}), \quad \text{and} \quad \Gamma'_{\mathscr{K}}(S) = \mathsf{lfp}(T_{\mathscr{K}^*_G/S})$$

Both operators are shown to be antitonic (Knorr *et al.* 2008), hence their composition is monotonic and form the basis for defining the well-founded MKNF model. Here we present its alternating computation.

$$\begin{array}{rr} \mathbf{T}_0 = \emptyset & \mathbf{TU}_0 = \mathsf{KA}(\mathscr{K}^*) \\ \mathbf{T}_{n+1} = \Gamma_{\mathscr{K}}(\mathbf{TU}_n) & \mathbf{TU}_{n+1} = \Gamma'_{\mathscr{K}}(\mathbf{T}_n) \\ \mathbf{T}_\omega = \bigcup \mathbf{T}_n & \mathbf{TU}_\omega = \bigcap \mathbf{TU}_n \end{array}$$

Note that by finiteness of the ground knowledge base (Definition 1) the iteration stops before reaching ω. It was shown in Knorr *et al.* (2008) that the sequences are monotonically increasing and decreasing respectively, and that $\mathbf{T}_\omega$ and $\mathbf{TU}_\omega$ form the well-founded model in the following sense.

Definition 7
Let $\mathscr{K} = (\mathscr{O}, \mathscr{P})$ be a DL-safe hybrid MKNF knowledge base and let $\mathbf{T}_{\mathscr{K}}, \mathbf{TU}_{\mathscr{K}} \subseteq \mathsf{KA}(\mathscr{K})$, with $\mathbf{T}_{\mathscr{K}}$ being $\mathbf{T}_\omega$ and $\mathbf{TU}_{\mathscr{K}}$ being $\mathbf{TU}_\omega$ both restricted to the modal atoms occurring in $\mathsf{KA}(\mathscr{K})$. Then

$$M_{WF} = \{\mathbf{K}\ A \mid A \in \mathbf{T}_{\mathscr{K}}\} \cup \{\mathbf{K}\ \pi(\mathscr{O})\} \cup \{\mathbf{not}\ A \mid A \in \mathsf{KA}(\mathscr{K}) \setminus \mathbf{TU}_{\mathscr{K}}\}$$

is the *well-founded MKNF model* of $\mathscr{K}$, where $\pi(\mathscr{O})$ denotes the first-order logic formula equivalent to the ontology $\mathscr{O}$ (for details on the translation of $\mathscr{O}$ into the first-order logic, see Motik and Rosati 2007).

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All modal **K**-atoms in M_{WF} are true, all modal **not**-atoms are false, and all other modal atoms from $\mathsf{KA}(\mathscr{K})$ are undefined.

As shown in Knorr *et al.* (2008), the well-founded model is sound with respect to the original semantics of Motik and Rosati (2007), i.e. all atoms true (resp. false) in the well-founded model are also true (resp. false) in the model of Motik and Rosati (2007). In fact, the relation between the semantics of Knorr *et al.* (2008) and Motik and Rosati (2007) is tantamount to that of the well-founded semantics and the answer-sets semantics of logic programs. Moreover, this definition is in fact a generalization of the original definition of the well-founded semantics of normal logic programs in the sense that if the ontology is empty, then this definition exactly yields the well-founded models according to van Gelder *et al.* (1991). For more properties, as well as motivation and intuitions on $MKNF_{WFS}$, the reader is referred to Knorr *et al.* (2008).

3 XSB Prolog and the Coherent Description Framework

Our implementation of $MKNF_{WFS}$ is based on XSB Prolog (`xsb.sourceforge.net`) for two reasons. First, XSB's tabling engine evaluates rules according to well-founded semantics, and ensures rule termination for programs and goals with the *bounded term-size property*.[5] Second, the implementation uses the prover from XSB's ontology management system, the CDF (Swift and Warren 2003).

Coherent Description Framework has been used in numerous commercial projects, and was originally developed as a proprietary tool by the company XSB Inc.[6] Since 2003, CDF has been used to support extraction of information about aircraft parts from free-text data fields, about medical supplies and electronic parts from web sites and electronic catalogs, and about the specifics of mechanical parts from scanned technical drawings. Also, CDF is used to maintain screen models for graphical user interfaces that are driven by XSB and its graphics package, XJ (`www.xsb.com/xj.aspx`). We discuss features of CDF that are relevant to the implementation described in Section 4.

3.1 Type-0 and Type-1 ontologies

All classes in CDF are represented by terms of the form *cid(Identifier, Namespace)*, instances by terms of the form *oid(Identifier, Namespace)*, and relations by terms of the form *rid(Identifier, Namespace)*, where *Identifier* and *Namespace* can themselves be any ground Prolog term.

Commercial use has driven CDF to support efficient query answering from Prolog for very large knowledge bases. A key to this is that ontologies in CDF can have a restricted, tractable form. *Type-0* ontologies do not allow representation

[5] Intuitively, a program P and goal G have the bounded term-size property if there is a finite number n such that all subgoals and answers created in the evaluation of the goal G to P have a size less than n.

[6] Most of CDF is open-source, including all features used in this paper. CDF is distributed as a package in XSB's standard release, and full details can be found in its accompanying manual.

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$Man \sqsubseteq Person \sqcap Male$	`isa(cid(man),cid(person))` `isa(cid(man),cid(male))`
$Husband \sqsubseteq Man \sqcap \exists Spouse.Person$	`isa(cid(husband),cid(man)).` `hasAttr(cid(husband),rid(spouse),cid(person)`
$adam : Husband$	`isa(oid(adam),cid(husband)`

Fig. 1. Some DL axioms and their Type-0 counterparts.

of negation or disjunction within the ontology itself, and implicitly use the closed-world assumption. As such, Type-0 ontologies resemble a frame-based representation more than a description logic, and do not add any complexity to query evaluation beyond that of well-founded semantics. Support for query answering motivates the representation of Type-0 ontologies. The predicate *isa*/2 is used to state inclusion: whether the inclusion is a subclass, element, or subrelation depends on the type of the term (not all combinations of types of terms are allowed in a CDF program). Relational atoms in CDF have the form:

- $hasAttr(Term_1, Rel_1, Term_2)$ which has the meaning $Term_1 \sqsubseteq \exists Rel_1.Term_2$;
- $allAttr(Term_1, Rel_1, Term_2)$ with the meaning $Term_1 \sqsubseteq \forall Rel_1.Term_2$;
- along with other forms that designate cardinality constraints on relations.

Figure 1 presents some DL axioms and their Type-0 counterparts, where namespace information has been omitted for readability. The fact that Type-0 ontologies cannot express negation is crucial to their ability to be directly queried. In other words, `isa/2`, `hasAttr/3` and other atoms can be called as Prolog goals, with any instantiation pattern for the call. Query answering for Type-0 goals checks inheritance hierarchies and does not rely on unification alone. Type-0 ontologies use tabling to implement inheritance and use tabled negation so that only the most specific attribute types for a `hasAttr/3` or other query are returned to a user.

Besides the constructs of Type-0 ontologies, Type-1 ontologies further allow atoms of the form

$$necessCond(Term_1, CE)$$

where CE can be any $\mathscr{ALC}2$ class expression over CDF terms. For instance, the axiom

$$Woman \sqsubseteq Person \sqcap \neg Man$$

would be represented by the atom

```
necessCond(cid(woman),(cid(person),neg(cid(man))))
```

where the comma represents conjunction, as in Prolog. Because they use open-world negation, atoms for Type-1 ontologies cannot be directly queried; rather they are queried through goals such as $allModelsEntails(Term, ClassExpr)$, succeeding if

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$Term \sqsubseteq ClassExpr$ is provable in the current state of the ontology. Type-1 ontologies deduce entailment using a tableau prover written in Prolog.

3.2 System features of CDF

Regardless of the type of ontology, atoms such as $isa/2$, $hasAttr/2$, etc. can be defined extensionally via Prolog atoms, or intensionally via Prolog rules. For instance, evaluation of the goal

```
hasAttr(Class1,Rel,Class2)
```

would directly check extensional Prolog facts through a subgoal

```
hasAttr_ext(Class1,Rel,Class2)
```

and would also check intensional rules through a subgoal

```
hasAttr_int(Class1,Rel,Class2)
```

Intensional definitions are used so that atoms can be lazily defined by querying a database or analyzing a graphical model: their semantics is outside that of CDF. In fact, using combinations of rules and facts, Type-0 ontologies are commonly used comprising tens of thousands of classes and relations, and tens of millions of statements about individuals. At the same time, intensional definitions in a Type-1 ontology provide a basis for the tableau prover to call rules, as is required to support the interdependencies of $MKNF_{WFS}$, and will be further discussed in Section 4.2.

Despite their restrictions, the vast majority of knowledge used by XSB Inc. is maintained in Type-0 ontologies. Although Type-0 ontologies have supported numerous commercial projects, their limitations of course preclude the full use of information in ontologies. Support of a uniform querying mechanism for individuals in $MKNF_{WFS}$ as described below is intended as a means to allow commercial projects to use a more powerful form of knowledge representation.

3.3 Related work

The Coherent Description Framework was originally developed in 2002–2003, and Type-0 ontologies were envisioned as a means to represent object-oriented knowledge in Prolog. Unlike Flora-2 (Yang *et al.* 2003), CDF was intended to be a Prolog library, and its inheritance was designed to be entirely monotonic for compatibility with description logics. Type-1 ontologies were originally evaluated through a translation into ASP (Swift 2004): this approach pre-dated that of KAON2 (Motik 2006) and was abandoned due to the difficulty of dynamically pruning search in ASP; afterwards the current tableau approach was developed which attempts to examine as small a portion of the ontology as possible when proving entailment (cf., e.g. Horrocks and Patel-Schneider (1999) for a discussion of how search may be pruned in tableau prov*a*ers for ontologies). CDF's approach may be distinguished from Lukacsy *et al.* (2008), which also combines ontological deduction with Prolog. Type-0 ontologies rely on WFS reasoning and so achieve good scalability under a weak

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semantics; theorem proving for Type-1 ontologies is used only when needed. Lukacsy *et al.* (2008) take a more uniform approach to deduction which relies on WAM-level extensions for efficiency; to our knowledge this approach is research-oriented, and has not been used commercially.

4 Goal-driven MKNF implementation

In Section 2 we presented a bottom-up computation that constructs the complete well-founded model for a given hybrid knowledge base. However, in practical cases, especially when considering the context of the Semantic Web, this is not what is intended. In fact, it would make little sense to compute the whole model of anything that is related to the World Wide Web. Instead, one would like to query the knowledge base for a given predicate (or propositional atom) and determine its true value. As an illustration, recall Example 1, where we wanted to know if a given shipment should be inspected or not when it arrived, or the case study of Patel *et al.* (2007), where one may want to know whether a given patient matches the criteria for a given trial. Deriving all the consequences of a knowledge base to answer a query about a given shipment or patient would be impractical.

In this section we describe the algorithms and the design of *CDF-Rules*, a goal-driven implementation for hybrid MKNF knowledge bases under the Well-Founded Semantics that minimizes the computation to the set of individuals that are relevant to a query. *CDF-Rules* makes use of XSB's tabled SLG Resolution (Chen and Warren 1996) for the evaluation of a query, together with tableaux mechanisms supported by CDF theorem prover to check entailment on the ontology. *CDF-Rules* is tuned for Type-1 ontologies, and thereby is also compatible with Type-0 ontologies. For the description of the solution, we assume that the reader has a general knowledge of tabled logic programs (cf. e.g. Swift and Warren 2012).

4.1 A query-driven iterative fixed point

At an intuitive level, a query to *CDF-Rules* is evaluated in a relevant (top-down like) manner through SLG resolution until the selected goal is a literal l formed over a DL-atom. At that point, in addition to further resolution, the ontology also uses tableau mechanisms to derive l. However, as a tableau proof of l may require propositions (literals) inferred by other rules, considerable care must be taken to integrate the tableau proving with rule-based query evaluation.

In its essence, a tableau algorithm decides the entailment of a formula φ with respect to an ontology $\mathcal{O}$ by trying to construct a common *model* for $\neg\varphi$ and $\mathcal{O}$, sometimes called a *completion graph* (cf. e.g. Schmidt-Strauss and Smolka 1990). If such a model can not be constructed, $\mathcal{O} \models \varphi$; otherwise $\mathcal{O}$ does not entail φ. Similar to other DL provers, the CDF theorem prover attempts to traverse as little of an ontology as possible when proving φ. As a result, when the prover is invoked on an atom A, the prover attempts to build a model for the underlying individual(s) to which A refers, and explores additional individuals only as necessary.

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For our purposes, given the particular interdependence between the rules and the ontology in $MKNF_{WFS}$, the prover must consider the knowledge inferred by the rules in the program for the entailment proof, as a DL-atom can be derived by rules, which in turn may rely on other DL-atoms entailed by the ontology. Thus, a query to a DL-atom $p(o)$ iteratively computes a (sub-)model for o, deriving at each iteration new information about the roles and classes of o, along with information about other individuals related to o either in the ontology (via CDF's tableau algorithm) or in the rules (via SLG procedures) until a fixed point is reached.

We start by illustrating a special case of positive knowledge bases without default negation in the rules.

Example 3

Consider the following KB (with the program on the left and the ontology on the right[7]) and the query $third(X)$:

$$\begin{array}{ll} \mathbf{K}\ third(X) \leftarrow p(X), \mathbf{K}\ second(X). & \\ \mathbf{K}\ first(callback). & First \sqsubseteq Second \\ p(callback). & \end{array}$$

The query resolves against the rule for $third(X)$, leading to the goals $p(X)$ and $\mathbf{K}\ second(X)$. The predicate p, although not a DL-atom, assures DL-safety, restricting the application of the rules to known individuals. The call $p(X)$ returns true for $X = callback$. Accordingly, the next subgoal is $\mathbf{K}\ second(callback)$ which depends on the DL-atom $second(callback)$, corresponding in the ontology to the proposition $Second$. At this point, the computation calls the CDF theorem prover which starts to derive a model for all the properties of the individual $callback$. Yet in this computation, the proposition $Second$ itself depends on a predicate defined in the rules – $First$. It can thus be seen that the evaluation of the query $third(callback)$ must be done iteratively – the (instantiated) goal $third(callback)$ should suspend (using tabling) until $second(callback)$ is resolved. Furthermore, $second(callback)$ needs first to prove $first(callback)$ from the rules. In general, goals to DL-atoms may need to suspend in order to compute an iterated fixed point, after which they may either succeed or fail.

To formalize the actions in Example 3 on the special case of definite programs, we start by considering the computation for all individuals (i.e. temporarily disregarding the relevance of individuals as discussed above).

Definition 8

Let $\mathscr{K} = (\mathscr{O}, \mathscr{P})$ be a DL-safe hybrid MKNF knowledge base, where $\mathscr{P}$ does not contain default negation. Let $\mathscr{I}$ be a fixed set of individuals. The function $Tableau(\mathscr{O})$ computes for a theory $\mathscr{O}$ the entailments of $\mathscr{O}$ for $\mathscr{I}$, disregarding the rules component. The function $SLG(\mathscr{P})$ computes via tabling the set of DL-atoms

[7] To simplify reading, for rules we omit **K** before non-DL atoms. In fact, in the implementation the ontology must be written according to CDF syntax, and in the rules the modal operators **K** and **not** are replaced by (meta-)predicates $known/1$ and $dlnot/1$ respectively (see Section 4.2).

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true in the minimal model of $\mathscr{P}$ for a set of individuals, $\mathscr{I}$, disregarding the ontology component. The model is obtained as the union of the least fixed point of sequences:

$$\begin{aligned} D_0 &= Tableau(\mathscr{O}) & R_0 &= SLG(\mathscr{P}) \\ D_1 &= Tableau(\mathscr{O} \cup R_0) & R_1 &= SLG(\mathscr{P} \cup D_0) \\ &\ldots & &\ldots \\ D_n &= Tableau(\mathscr{O} \cup R_{n-1}) & R_n &= SLG(\mathscr{P} \cup D_{n-1}) \end{aligned}$$

Definition 8 resembles Definition 4 of the operator $T_{\mathscr{K}}$ in Section 2. In fact, the R_i sequence is similar to the $R_{\mathscr{K}}(S)$ operator which collects new conclusions from the rules, whereas the D_i sequence is similar to the $D_{\mathscr{K}}(S)$ operator which collects new conclusions from the ontology. Rather than starting with an empty set of conclusions from the rules, as is the case for $T_{\mathscr{K}}$ of Definition 4, here the R_i sequence starts with all conclusions that can be drawn from the program alone.[8] Given these minor differences, taking the function $Tableau(\mathscr{O})$ as correct with respect to the consequence relation of the description logic in use, and taking the function $SLG(\mathscr{P})$ as correct with respect to the least model semantics of definite logic programs, it is easy to see that if $\mathscr{I}$ is the set of all individuals in the knowledge base, then the union of the D_n and R_n at the fixed point exactly coincides with the least fixed point of $T_{\mathscr{K}}$. Furthermore, as long as the program P respects DL-safety, MKNF rules are lazily grounded with respect to the set of individuals $\mathscr{I}$. In fact, given a DL-safe set of MKNF rules, and a set of queries grounded with the individuals in $\mathscr{I}$, the evaluation of the queries results in a complete grounding of the rules, and so the fixed point is guaranteed in a finite number of steps.

Definition 8 captures certain aspects of how the rules and the ontology use each other to derive new knowledge in *CDF-Rules* via an alternating computation between the rules and the ontology. However, it does not capture cases in which the relevant set of individuals changes (i.e. it does not deal with changes in the set $\mathscr{I}$), or the presence of default negation in rule bodies. With regard to relevant individuals, since it is possible both to define n-ary predicates in rules and roles in the ontology, a query may depend on several individuals. Therefore, the fixed point computation must take into account the entire set of individuals that the query depends upon. This is done by tabling information about each individual in the set of individuals relevant to the query. This set may increase throughout the fixed point iteration as new dependency relations between individuals (including equality) are discovered. The iteration stops when it is not possible to derive anything else about these individuals, i.e. when both the set of individuals and the classes and roles of those individuals have reached a fixed point. The details of this iterative increase in the set of considered individuals can be found in the algorithm of Figure 2, which also addresses default negation and its interplay with the first-order negation.

The following example considers the presence of default negation in rule bodies.

[8] Since $T_{\mathscr{K}}$ is monotonic, it is clear that starting the iteration of this operator with all conclusions drawn from the rules alone would yield exactly the same (least) fixed point.

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Example 4
Consider the following knowledge base:

$\mathbf{K}\ fourth(X) \leftarrow p(X), \mathbf{not}\ \ third(X).$	$Fourth \sqsubseteq Fifth$
$\mathbf{K}\ third(X) \leftarrow p(X), \mathbf{K}\ second(X).$	$First \sqsubseteq Second$
$\mathbf{K}\ first(callback).$	
$p(callback).$	

In this example a predicate $fourth(X)$ is defined as the default negation of $third(X)$. Since $fourth(X)$ is defined in the rules, the negation is *closed world*, that is $fourth(X)$ should only succeed if it is not possible to prove $third(X)$. Consequently, if we employed SLG resolution blindly, an iteration where the truth of $second(callback)$ had not been made available to the rules from the ontology might mistakenly fail the derivation of $third(callback)$ and so succeed $fourth(callback)$. Likewise, the rules may pass to the ontology knowledge that after some iterations no longer applies – in this case if the ontology were told that $fourth(callback)$ was true, it would mistakenly derive *Fifth*.

Example 4 illustrates the need to treat default negation carefully, as the truth of default literals requires re-evaluation when new knowledge is inferred. Recall the manner in which the operators $\Gamma_{\mathscr{K}}$ and $\Gamma'_{\mathscr{K}}$ of Definition 6 address the problem of closed-world negation. Roughly, one step in $\Gamma_{\mathscr{K}}$ (or $\Gamma'_{\mathscr{K}}$) is defined as the application of $T_{\mathscr{K}}$ until reaching a fixed point. Applying $\Gamma'_{\mathscr{K}}$ followed by $\Gamma_{\mathscr{K}}$ is a monotonic operation and thus is guaranteed to have a least fixed point. In each dual application of $\Gamma_{\mathscr{K}}$ and $\Gamma'_{\mathscr{K}}$ two different models follow – a monotonically increasing model of true atoms (i.e. true predicates and propositions), and a monotonically decreasing model of non-false atoms.

In a similar way, the implementation of *CDF-Rules* makes use of two fixed points: an *inner* fixed point where we apply Definition 8 corresponding to $T_{\mathscr{K}}$; and an *outer* fixed point for the evaluation of **not**s, corresponding to $\Gamma_{\mathscr{K}}$ (and $\Gamma'_{\mathscr{K}}$). In the outer iteration, the evaluation of closed-world negation is made by a reference to the previous model obtained by $\Gamma_{\mathscr{K}}$. Thus, in *CDF-Rules*, $\mathbf{not}(A)$ succeeds if, in the previous *outer* iteration, A was not proven.

Example 5
To illustrate the need to apply two fixed points, consider the knowledge base below and the query $c(X)$:

$\mathbf{K}\ c(X) \leftarrow p(X), \mathbf{K}\ a(X), \mathbf{not}\ b(X).$	$A \sqsubseteq B$
$\mathbf{K}\ a(object).$	
$p(object).$	

When evaluating the query $c(X)$, X is first bound to $object$ by p, and then the nested iteration begins. The inner iteration follows the steps of Definition 8, and since these operators are defined only for definite rules, each negative body literal in a rule such as $p(X)$ is evaluated according to its value in the previous *outer* fixed point, or is simply evaluated as *true* in the first outer iteration. (As we will see, this is done lazily by *CDF-Rules*.) The first stage of the inner iteration computes

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$R_0 = \{a(object), p(object), c(object)\}$ (Definition 8) via the rules; and computes via the ontology $D_0 = \emptyset$, as $\mathcal{O} \not\models A$. In the second inner stage the rules achieve the same fixed point as in the first, so $R_1 = R_0$, but the ontology derives $object : B$ in D_1. After sharing this knowledge, there is nothing else to infer by either components, and we achieve the first inner fixed point with

$$T_1 = \{a(object), b(object), c(object), p(object)\}$$

So now the second outer iteration starts the computation of the inner iteration again, and in this iteration negative literals in the rules are evaluated with respect to T_1. As a consequence, $c(object)$ fails, since $b(object) \in T_1$. The fixed point of the second inner iteration contains $p(object)$, $a(object)$, and $b(object)$, which is in fact the correct model for $object$. Afterwards, a final outer iteration is needed to determine that an outer fixed point has in fact been reached. Since $c(object)$ is in the model of the final iteration, the query $c(X)$ succeeds for $X = object$.

The procedure to compute a lazily invoked iterative fixed point over a DL-safe MKNF hybrid knowledge base is summarized in Figure 2 using predicates that are described in detail in Section 4.2. In each inner iteration, the tabled predicate $known/3$ is used to derive knowledge from the rules component, while $allModelsEntails/3$ infers knowledge from the ontology via tableau proofs. Within rules evaluated by $known/3$, the default negation of a DL-atom A is obtained by the predicate $dlnot(A)$, which succeeds if A was not proven in the last outer iteration. The predicates $definedClass/2$ and $definedRole/3$ are used to obtain the relevant classes and roles defined for a given individual. We assume that these predicates are defined explicitly by the compiler or programmer, but these can also be inferred via the DL-safe restriction.[9] Regardless of whether inference is used, whenever a role is encountered for an individual, a check is made to determine whether the related individual $Individual_1$ is already in the list of individuals in the fixed point, and $Individual_1$ is added if not.

In order to compute $MKNF_{WFS}$, the algorithm shown in Figure 2 must create two different sets (cf. Definition 7): a credulous set, TU, containing the atoms that are true or undefined corresponding to application of the operator $\Gamma'_{\mathcal{K}}$; and a skeptical set, T, of the atoms that are true corresponding to $\Gamma_{\mathcal{K}}$ (Definition 6). The iterations in Figure 2 capture the construction of these sets in the following manner. The first iteration of $OutIter$ in $known(Term, OutIter, InIter)$ (where $OutIter = 0$) corresponds to the first step of computation of the set TU, whereas the second iteration corresponds to the second step of computation of the set T. As a consequence, iterations where $OutIter$ is indexed with an even number are monotonically decreasing TU iterations, while iterations indexed with an odd number are monotonically increasing T iterations. By making use of this property, the algorithm of Figure 2 ensures that the fixed point will only be achieved in TU iterations. This way, $Query$ is true if $known(Query, Outer_{Final} - 1, Inner_{Final})$ holds.

[9] Because of DL-safety, every DL-rule must contain a positive literal that is *only* defined in the rules. Such a literal limits the evaluation of the rules to known individuals so that *CDF-Rules* can infer the set of individuals that are applicable to a given rule.

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```
   Input: A query Query to a DL-Atom
   Output: Value of the input query in MKNF_WFS
 1 addIndividuals(Query,IndividualList);
 2 foreach Individual in IndividualList do
 3 |  OutIter, InIter = 0;
 4 |  S = S_1 = {};
 5 |  P = P_1 = {};
 6 |  repeat
 7 |  |  P = P_1;
 8 |  |  repeat
 9 |  |  |  S = S_1;
10 |  |  |  foreach Class in definedClass(Individual,Class) do
11 |  |  |  |  Term = Class(Individual);
12 |  |  |  |  S_1 = S_1 ∪ known(Term, OutIter, InIter);
13 |  |  |  |  S_1 = S_1 ∪ allModelsEntails(Term, OutIter, InIter);
14 |  |  |  |  S_1 = S_1 ∪ allModelsEntails(neg(Term), OutIter, InIter);
15 |  |  |  end
16 |  |  |  foreach Role in definedRole(Individual,Individual_1,Role) do
17 |  |  |  |  Term = Role(Individual,Individual_1);
18 |  |  |  |  add Individual_1 to IndividualList if necessary
19 |  |  |  |  S_1 = S_1 ∪ known(Term, OutIter, InIter);
20 |  |  |  |  S_1 = S_1 ∪ allModelsEntails(Term, OutIter, InIter);
21 |  |  |  |  S_1 = S_1 ∪ allModelsEntails(neg(Term), OutIter, InIter);
22 |  |  |  end
23 |  |  |  InIter++;
24 |  |  until S = S_1 ;
25 |  |  P = S;
26 |  |  OutIter++;
27 |  until OutIter is even (a TU evaluation) and P = P_1 ;
28 end
29 if known(Query,Outer_Final-1,Inner_Final) then
30 |  return true
31 else
32 |  if known(Query,Outer_Final,Inner'_Final) then
33 |  |  return undefined
34 |  else
35 |  |  return false
36 |  end
37 end
```

Fig. 2. The top-level algorithm: *ComputeFixedPoint(Query)*.

If this is not the case, then *Query* is undefined if $known(Query, Outer_{Final}, Inner_{Final})$ holds, otherwise *Query* is false.

4.2 *Implementing* $\mathbf{MKNF}_{WFS}$ *components*

We now describe various predicates in the algorithm of Figure 2, including the manner in which the rule and ontology components exchange knowledge, and how the fixed point is checked.

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```
known(A):-
     computeFixedPoint(A),
     get_object_iter(A,OutIter,InIter),
     known(A,OutIter,InIter).

:- table known/3.
known(A,OutIter,InIter):-
  PrevIter is InIter - 1,
  (   call(A),
    ;
      InIter > 0,
      allModelsEntails(A,OutIter,PrevIter)
  ),
  ( OutIter mod 2 =:= 1 ->
        true
      ;
        no_prev_neg(A,OutIter, PrevIter)
  ).

/* Enforce coherence of default negation with first-order
    negation */
no_prev_neg(_A,_OutIter, PrevIter) :-
  PrevIter < 0,!.
no_prev_neg(A,OutIter, PrevIter) :-
  tnot(allModelsEntails(neg(A),OutIter,PrevIter)).
```

Fig. 3. Prolog implementation of **K** for class properties.

4.2.1 Rules component

As mentioned, rules are transformed to use $known/1$ corresponding to **K** and $dlnot/1$ corresponding to **not**. As shown in Figure 3, given the goal $known(A)$ with $A = p(O)$, the code first calls $computeFixedPoint(p(O))$ to perform the fixed point computation for the object instance O. As in Figure 2, $computeFixedPoint(p(O))$ calls the lower-level $known/3$ and $dlnot/3$ to determine the truth of literals during the fixed point computation. Once the fixed point has been reached, $known/1$ uses *get_object_iter(p(O),Outer,Inner)* to obtain the final iteration indices for O from a global store, and calls $known/3$ again to determine the final truth value of $p(O)$. Note that $known/3$ is always called with the iteration indices (arguments 2 and 3) bound so that these are always contained in the table entries. Thus, the post-fixed point call to $known/3$ simply checks the table, and is not computationally expensive.

Within a given iteration, $p(O)$ may be known in one of the two ways. Either it can be directly derived from the rules; or $O \in P$ (i.e. $o{:}P$) may have been entailed by the ontology in the previous inner iteration step, as determined by the call $allModelsEntails(p(O), OutIter, PrevIter)$. In either case, care must be taken so that if $\neg A$ holds, then **not** A holds as well. In the formalism of Definition 3 this is guaranteed in two steps. First, an axiom $\neg P \sqsubseteq NP$ is added for each DL-atom that occurs in the head of a rule; in addition, the literal **not** NP is added in the body

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```
dlnot(A):-
     computeFixedPoint(A),
     get_object_iter(A,OutIter,_InIter),
     dlnot(A,OutIter).

/* In first iteration, ensure that TU = KA(K*) */
dlnot(_A,0):- !.
/* In subsequent iterations, check previous outer iteration */
dlnot(A,OutIter):-
        PrevIter is OutIter - 1,
        get_final_iter(A,PrevIter,FinIter),
        tnot(known(A,PrevIter,FinIter)).
```

Fig. 4. Prolog implementation of **not** for class properties.

of each rule with head P: this rewrite is used by the $\Gamma'_{\mathscr{K}}$ operator to produce the TU set. Accordingly, in Figure 3 when we try to derive $known(A, OutIter, InIter)$ and $OutIter$ is even (i.e. corresponding to a TU step via $\Gamma'_{\mathscr{K}}$ in Definition 7), we check whether the ontology derived $\neg A$ in the previous inner iteration by the call $no_prev_neg(A, OutIter, PrevIter)$. If $\neg A$ was derived, then $no_prev_neg/3$ fails via the call to $tnot/1$ (which is XSB's operator for tabled negation), and the top-level goal also fails.

On the other hand, the predicate $dlnot(A)$, which uses closed-world assumption, succeeds if A fails (Figure 4). As discussed in Example 5, the evaluation of $dlnot/2$ must take into account the result of the previous *outer* iteration. Accordingly, in Figure 4 the call $dlnot(A)$ with $A = p(O)$ gets the current outer iteration for O, and immediately calls $dlnot/2$. If the outer iteration index is greater than 1, the second clause of $dlnot/2$ simply finds the index of the (inner) fixed point of the previous outer iteration, and determines whether A was true in that fixed point. Since the call to $known/3$ in $tnot/1$ is tabled, *dlnot/[1,2]* does not need to be tabled itself. As described before, outer iterations alternately represent iterations of T and TU sets of Definition 7, where T sets are monotonically increasing while TU sets are monotonically decreasing. To assure that the first TU set is the largest set ($\mathsf{KA}(\mathscr{K}^*)$ following Definition 6), we compel all calls to $dlnot/1$ to succeed in the first outer iteration, as represented by the first clause of $dlnot/2$.

4.2.2 Ontology component

The tabled predicate *allModelsEntails/3* provides interface to CDF's tableau theorem prover (Figure 5). It is called with an atom or its classical negation, and with its iteration indices bound. Although the iterations are not used in the body of *allModelsEntails/3*, representing the iteration information in the head ensures that its availability in table entries for use by *known/3*. *allModelsEntails/3* first converts the atomic form of a proposition to one used by CDF. That is, it translates a 1-ary DL-atom representing an individual's class membership to the CDF predicate *isa*/2, and a 2-ary DL-atom representing an individual's role to the CDF predicate

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```
:- table allModelsEntails/3.
allModelsEntails(neg(Atom),_OutIter,_InIter):- !,
        /* transform Atom to CDF object identifier and
           class expression*/
        /* add individuals to current fixed point list */
        (rec_allModelsEntails(Id,CE) -> fail ; true).
allModelsEntails(Atom,_OutIter,_InIter):-
        /* transform Atom to CDF object identifier and
           class expression*/
        /* add individuals to current fixed point list */
        (rec_allModelsEntails(Id,neg(CE)) -> fail ; true).
```

Fig. 5. Prolog pseudo-code for *allmodelsEntails*/3.

hasAttr/3 (see Section 3). In addition, if *Atom* is a 2-ary role, the target individual may be added to the fixed point set of individuals. As is usual with tableau provers, entailment of a formula φ by an ontology $\mathcal{O}$ is shown if the classical negation of φ is inconsistent with $\mathcal{O}$. Thus, *rec_alModelsEntails*/*2* immediately fails if the classical negation of φ is consistent with $\mathcal{O}$ in the present iteration; otherwise, φ is entailed.

The tableau prover, called by *rec_allModelsEntails*/2, obtains all information inferred by the rules during the previous inner iteration in accordance with Definition 8. This is addressed via the CDF intensional rules. As discussed in Section 3, the architecture of a CDF instance can be divided into two parts – extensional facts and intensional rules. Extensional facts define CDF classes and roles as simple Prolog facts; intensional rules allow classes and roles to be defined by Prolog rules that are outside of the $MKNF_{WFS}$ semantics. In our case, the intensional rules support a programming trick to check rule results from a previous iteration. As shown in Figure 6, these convert the CDF form of an ontology axiom into a 1-ary or 2-ary predicate, and then check the *known*/3 table for a previous iteration using the predicate *lastKnown*/*1* (not shown). If roles or classes are uninstantiated in the call from the tableau prover, all defined roles and classes for the individual are instantiated using *definedClass*/*3* or *definedRole*/*4* before calling *lastKnown*/*1*.

4.2.3 Usage

An MKNF hybrid knowledge base is defined over a XSB-Prolog knowledge base together with an ontology specified over CDF. In *CDF-Rules* such a knowledge base is written into two files as follows:

- *rules.P* – Containing the set of MKNF rules and facts. A rule is defined as standard Prolog rules as follows:

  `Head :-` A_1`, ...`A_k`,known(`B_1`),...,known(`B_n`),dlnot(`C_1`),...,dlnot(`C_m`).`

  where $k, n, m \geqslant 0$, and the A_is are all non-DL predicates (i.e. predicates that are not defined in the ontology), and the B_is and C_is are predicates that can be both defined in the rules and in the ontology. If $k = n = m = 0$, then the rule is a fact, and it is written as usual in Prolog, omitting the ':-' operator.

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```
isa_int(oid(Obj,NS),cid(Class,NS1)):-
    ground(Obj),ground(Class),!,
    Call =.. [Class,Obj],          /* Call = Class(Obj) */
    lastKnown(Call).
/* Find all possible classes for Obj if called with superclass
   argument uninstantiated */
isa_int(oid(Obj,NS),cid(Class,NS)):-
    ground(Obj),var(Class),!,
    definedClass(Call,Class,Obj),
    lastKnown(Call).

hasAttr_int(oid(Obj1,NS),rid(Role,NS1),oid(Obj2,NS2)):-
    ground(Obj1), ground(Obj2), ground(Role),!,
    Call =.. [Role,Obj1,Obj2],     /* Call = Role(Obj1,Obj2) */
    last_known(Call).
/* Find all possible rules for Obj if called with role argument
    uninstantiated */
hasAttr_int(oid(Obj1,NS),rid(Role,NS1),oid(Obj2,NS2)):-
    ground(Obj1), ground(Obj2), var(Role),!,
    definedRole(Call,Role,Obj1,Obj2),
    last_known(Call).
```

Fig. 6. Callbacks from the ontology component to the rules component.

Note that the transformation to include the negation *N_Head* in the body of a rule for *Head* as specified in Definition 3 is not needed: such a check is done by the call to `no_prev_neg/3` in `known/3`.

To guarantee correctness, each rule must respect DL-safety. However, in the current implementation it is the programmer's responsibility to check for this condition. The current implementation also does not check that the A_i predicates (i.e. the ones not under *known*/1 or *dlnot*/1) are not defined in the ontology. If a programmer opts to not precede the predicate by *known*/1 or *dlnot*/1, any definition for the predicate in the ontology is simply ignored.

- *cdf_extensional.P* – Comprising ordinary ontology facts and concepts defined over the CDF syntax.
- *cdf_intensional.P* – Containing predicates allowing the ontology to access information in the rules as in Figure 6. In addition, the file may contain other intensional rules to lazily access information from a database, off of the semanitc web, or from other sources external to *CDF-Rules*.

Example 6

The knowledge base of Example 1 can be easily coded in *CDF-Rules* as:

```
%rules
inspect(X) :- hasShipment(X,C), dlnot(safeCountry(C)).

%cdf_extensional
isa_ext(cid(scandinavianCtr,ont),cid(safeCountry,ont)).
isa_ext(cid(scandinavianCtr,ont),cid(EuropeanCtr,ont)).
```

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```
isa_ext(oid(norway,ont),cid(scandinavianCtr,ont)).
necesscond_ext(cid(DiplomaticShipt,ont),neg(cid(inspect,ont))).
```

Note that the ontological portion is Type-1 due to the use of `necessCond/2`.

4.2.4 Discussion

As described, *CDF-Rules* implements query answering to hybrid MKNF knowledge bases, and tries to reduce the amount of relevance required in the fixed point operation. Relevance is a critical concept for query answering in practical systems; however, a poorly designed ontology or rules component can work against one another if numerous individuals depend on one another through DL roles. In such a case the relevance properties of our approach will be less powerful; however, in such a case a simple query to an ontology about an individual will be inefficient in itself. The approach of *CDF-Rules* cannot solve such problems; but it can make query answering as relevant as the underlying ontology allows.

We do not present here a formal proof of soundness and completeness for our algorithm, since this would require the full presentation of formal derivation procedures on which both XSB-Prolog and CDF implementations rely. However, we have given an informal argument along with our description by referring to complementarity between the implementation and the bottom-up definition of $MKNF_{WFS}$. In particular, there is a close correspondence between the inner fixed points of our computation represented in Definition 8 and the $R_{\mathscr{K}}$, $D_{\mathscr{K}}$, and $T_{\mathscr{K}}$ operators of Definition 4; a correspondence between the actions of `known/3` in Figure 3 and the transformation of Definition 5 to ensure coherency between classical and default negation; and also a correspondence between our outer fixed points and the operators $\Gamma_{\mathscr{K}}$ / $\Gamma'_{\mathscr{K}}$. As a result, one can view our goal-driven implementation as an optimization of the bottom-up approach where the computation is limited to the set of *relevant* objects, and where the evaluation of positive predicates and the handling of iterations is performed by the use of SLG resolution.

Further optimizations of the described approach are possible. First is to designate a set of atoms whose value is defined *only* in the ontology: such atoms would require tableau proving, but could avoid the fixed point check of *computeFixedPoint*/1. Within *computeFixedPoint*/1 another optimization would be to maintain dependencies among individuals. Intuitively, if individual I_1 depended on individual I_2 but not the reverse, a fixed point for I_2 could be determined before that of I_1. However, these optimizations are fairly straightforward elaborations of *CDF-Rules* as presented.

5 Conclusions

In this paper we have described the implementation of a query-driven system, *CDF-Rules* for hybrid knowledge bases combining both (non-monotonic) rules and a (monotonic) ontology. The system answers queries according to $MKNF_{WFS}$ (Knorr *et al.* 2008) and, as such, is also sound with respect to the semantics defined in Motik and Rosati (2007) for hybrid MKNF knowledge bases. The definition of

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$MKNF_{WFS}$ is parametric on a decidable description logic (in which the ontology is written), and it is worth noting that, as shown in Knorr et al. (2008), the complexity of reasoning in $MKNF_{WFS}$ is in the same class as that in the decidable description logic; a complexity result that is extended to a query-driven approach in Alferes *et al.* (2012). In particular, if the description logic is tractable then reasoning in $MKNF_{WFS}$ is also tractable. Our implementation fixes the DL part to CDF ontologies that in its Type-1 version supports $\mathscr{ALQ}\mathscr{Q}$ description logic. CDF Type-0 ontologies are simpler and tractable, and, when using Type-0 ontologies only, our implementation exhibits a polynomial complexity behavior. This fact derives from the usage of tabling mechanisms, as defined in SLG resolution and implemented in XSB Prolog.[10] In fact, one of the reasons that highly influenced the choice of CDF as the parameter ontology logic in our query-driven implementation for hybrid MKNF knowledge bases was the very existence of an implementation of CDF relying on tabling that could be coupled together with the tabling we needed for $MKNF_{WFS}$. But the algorithms presented here do not rely on particularities of CDF, and we believe that, for other choices of parameter logics, implementations could be made in a way similar to the one described in this paper. Of course, such an implementation would require first an implementation in XSB-Prolog of a prover for the other description logic of choice, providing at least a predicate $allModelsEntails/3$ with the meaning as described above.

Though our choice for the implementation was $MKNF_{WFS}$ (Knorr *et al.* 2008), there were other formalisms concerned with combining ontologies with WFS rules (Eiter *et al.* 2004b; Drabent and Małuszynski 2007). The approach of Eiter *et al.* (2004b) combines ontologies and rules in a modular way, i.e. keeps both parts and their semantics separate, thus having similarities with $MKNF_{WFS}$. The interface for this approach is done by the `dlv-hex` system (Schindlauer 2006). Though with identical data complexity to $MKNF_{WFS}$ for a tractable DL, it has a less strong integration, having limitations in the way the ontology can call back program atoms (see Eiter *et al.* 2004b for details). Hybrid programs of Drabent and Maluszynski (2007) are even more restrictive: This formalism only allows the transfer of information from the ontology to the rules and not the other way around. Moreover, the semantics of this approach differs from MKNF (both the one of Motik and Rosati (2007) and $MKNF_{WFS}$) and also Eiter *et al.* (2004b) in that if an ontology expresses $B_1 \vee B_2$ then the semantics in Drabent and Maluszynski (2007) derives p from rules $p \leftarrow B_1$ and $p \leftarrow B_2$, p whereas MKNF and Eiter *et al.* (2004b) do not. For further comparisons of MKNF with other proposals, including those not based on WFS rules, see Motik and Rosati (2007) and Knorr *et al.* (2008), and for a survey on other proposals for combining rules and ontologies, see Hitzler and Parsia (2009).

CDF-Rules serves as a proof-of-concept for querying $MKNF_{WFS}$ knowledge bases. As discussed, XSB and tractable CDF ontologies have been used extensively in commercial semantic web applications; the creation of *CDF-Rules* is a step toward

[10] The proof of tractability of the implementation of *CDF-Rules* with CDF Type-0 ontologies is beyond the scope of this paper.

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understanding whether and how $MKNF_{WFS}$ can be used in such applications. As XSB is multi-threaded, *CDF-Rules* can be extended to a $MKNF_{WFS}$ server in a fairly straightforward manner. Since XSB supports CLP, further experiments involve representing temporal or spatial information in a hybrid of ontology, rules, and rule-based constraints. In addition, since the implementation of both Flora-2 (Yang *et al.* 2003) and Silk (Grosof 2009) are based on XSB, *CDF-Rules* also forms a basis for experimenting with $MKNF_{WFS}$ on these systems.

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